

# Weakly-Supervised Learning with Cost-Augmented Contrastive Estimation

Kevin Gimpel

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- New objective for weakly-supervised NLP, generalizes contrastive estimation ([Smith & Eisner, 2005](#))
- Adds two cost functions: inputs and outputs
- Improved system combination for POS tagging

	many-to-1 accuracy	1-to-1 accuracy
Contrastive Estimation	61.8	47.2
Cost-Augmented Contrastive Estimation	<b>64.3</b>	<b>51.7</b>

avg. across 5 languages,  
PASCAL 2012 POS shared task

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# EM and Contrastive Estimation

Modification 1: Input Cost

Modification 2: Output Cost

# Generative Log-Linear Models

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word sequence

part-of-speech tag sequence

The diagram illustrates the inputs to a generative log-linear model. It shows the probability distribution  $p_{\theta}(x, y)$  as a function of two sequences: a word sequence and a part-of-speech tag sequence. The word sequence is mapped to the feature vector  $f(x, y)$ , and the part-of-speech tag sequence is mapped to the feature vector  $f(x', y')$ . The numerator of the formula represents the product of the weight vector  $\theta$  and the feature vector  $f(x, y)$ , while the denominator is a normalization factor representing the sum of the products of  $\theta$  and all possible feature vectors  $f(x', y')$ .

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word sequence

part-of-speech tag sequence

parameters

feature vector

# Generative Log-Linear Models

$$p_{\theta}(x, y) = \frac{\exp \{ \theta^\top f(x, y) \}}{\sum_{x'} \sum_{y'} \exp \{ \theta^\top f(x', y') \}}$$

$$\text{score}(x', y')$$

# Unsupervised Learning for Log-Linear Models

$$\boldsymbol{\theta}^* = \operatorname{argmax}_{\boldsymbol{\theta}} \sum_i \text{gain}(\mathbf{x}^{(i)}, \boldsymbol{\theta})$$

# EM

$$\text{gain}_{\text{EM}}(\boldsymbol{x}^{(i)}, \boldsymbol{\theta}) = \log \sum_{\boldsymbol{y}} p_{\boldsymbol{\theta}}(\boldsymbol{x}^{(i)}, \boldsymbol{y})$$

# EM

$$\begin{aligned} \text{gain}_{\text{EM}}(\boldsymbol{x}^{(i)}, \boldsymbol{\theta}) &= \log \sum_{\boldsymbol{y}} p_{\boldsymbol{\theta}}(\boldsymbol{x}^{(i)}, \boldsymbol{y}) = \\ &\log \sum_{\boldsymbol{y}} \exp \left\{ \text{score}(\boldsymbol{x}^{(i)}, \boldsymbol{y}) \right\} - \log \sum_{\boldsymbol{x}' \in \mathcal{X}} \sum_{\boldsymbol{y}'} \exp \left\{ \text{score}(\boldsymbol{x}', \boldsymbol{y}') \right\} \end{aligned}$$

# EM

$$\text{gain}_{\text{EM}}(\mathbf{x}^{(i)}, \boldsymbol{\theta}) = \log \sum_{\mathbf{y}} p_{\boldsymbol{\theta}}(\mathbf{x}^{(i)}, \mathbf{y}) =$$

$$\underbrace{\log \sum_{\mathbf{y}} \exp \left\{ \text{score}(\mathbf{x}^{(i)}, \mathbf{y}) \right\}}_{\text{reward all y's for observed x}} - \underbrace{\log \sum_{\mathbf{x}' \in \mathcal{X}} \sum_{\mathbf{y}'} \exp \left\{ \text{score}(\mathbf{x}', \mathbf{y}') \right\}}_{\text{penalize all y's for ALL x's}}$$

# Contrastive Estimation (CE)

(Smith & Eisner, 2005)

$$\text{gain}_{\text{CE}}(\mathbf{x}^{(i)}, \boldsymbol{\theta}) = \log \sum_{\mathbf{y}} p_{\boldsymbol{\theta}}(\mathbf{x}^{(i)}, \mathbf{y} \mid \mathcal{N}(\mathbf{x}^{(i)}))$$



“corruption neighborhood”

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reward all y's for observed x  
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reward all  $\mathbf{y}$ 's for observed  $\mathbf{x}$   
(same as EM)

penalize all  $\mathbf{y}$ 's for  $\mathbf{x}$ 's in  
corruption neighborhood

With well-designed neighborhood, CE shown effective for:

part-of-speech tagging (Smith & Eisner, 2005a)

dependency parsing (Smith & Eisner, 2005b)

morphological segmentation (Poon et al., 2009)

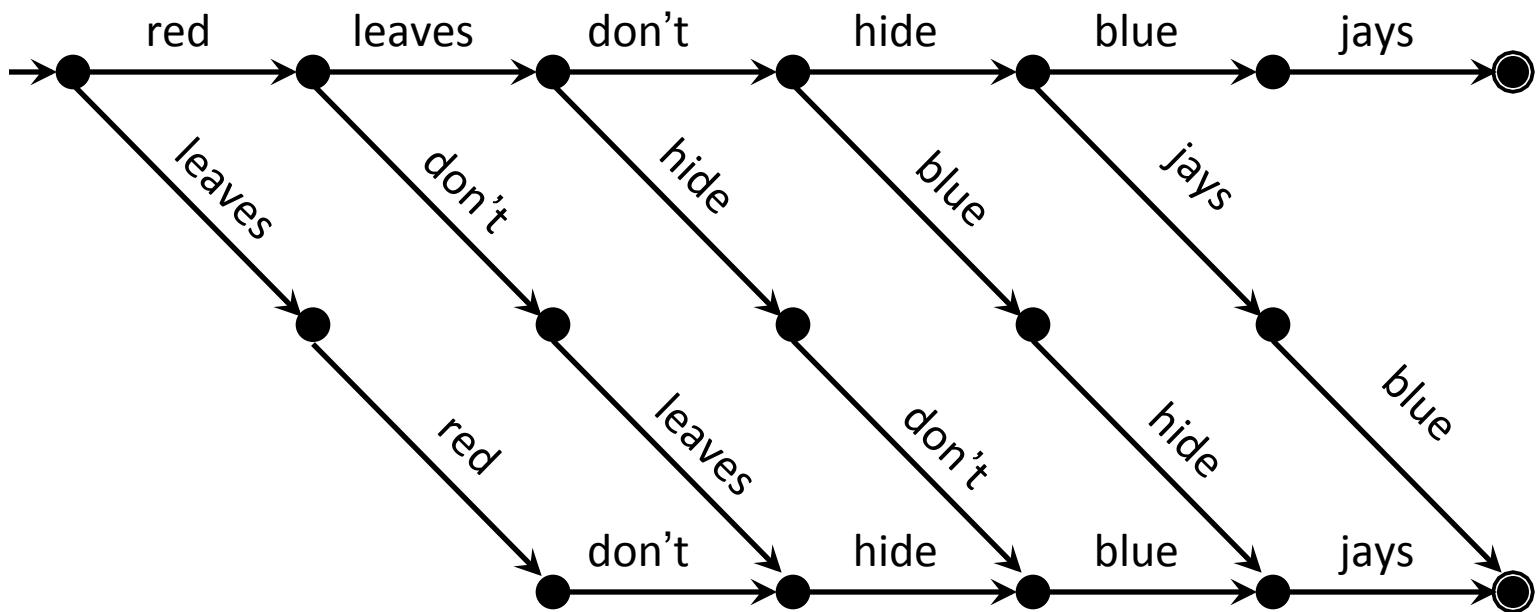
bilingual part-of-speech induction (Chen et al., 2011)

machine translation (Xiao et al., 2011)

# “Transpose1” Neighborhood

**Sentence:** red leaves don't hide blue jays

**Neighborhood:**



Smith & Eisner (2005)

# EM and Contrastive Estimation

Modification 1: Input Cost

Modification 2: Output Cost

# Contrastive Estimation:

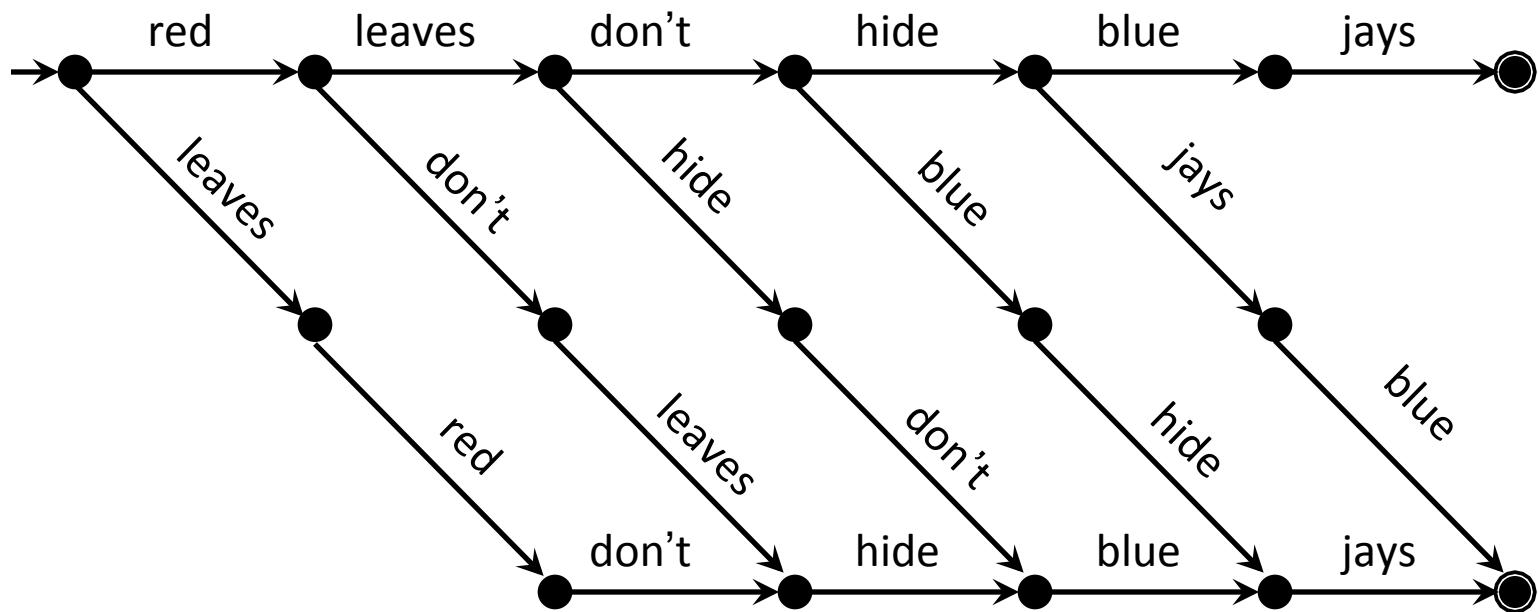
$$\log \sum_{\mathbf{y}} \exp \left\{ \text{score}(\mathbf{x}^{(i)}, \mathbf{y}) \right\} - \log \sum_{\mathbf{x}' \in \mathcal{N}(\mathbf{x}^{(i)})} \sum_{\mathbf{y}'} \exp \left\{ \text{score}(\mathbf{x}', \mathbf{y}') \right\}$$

all x's in corruption neighborhood  
treated equally!

# Transpose1 Neighborhood

**Sentence:** red leaves don't hide blue jays

**Neighborhood:**



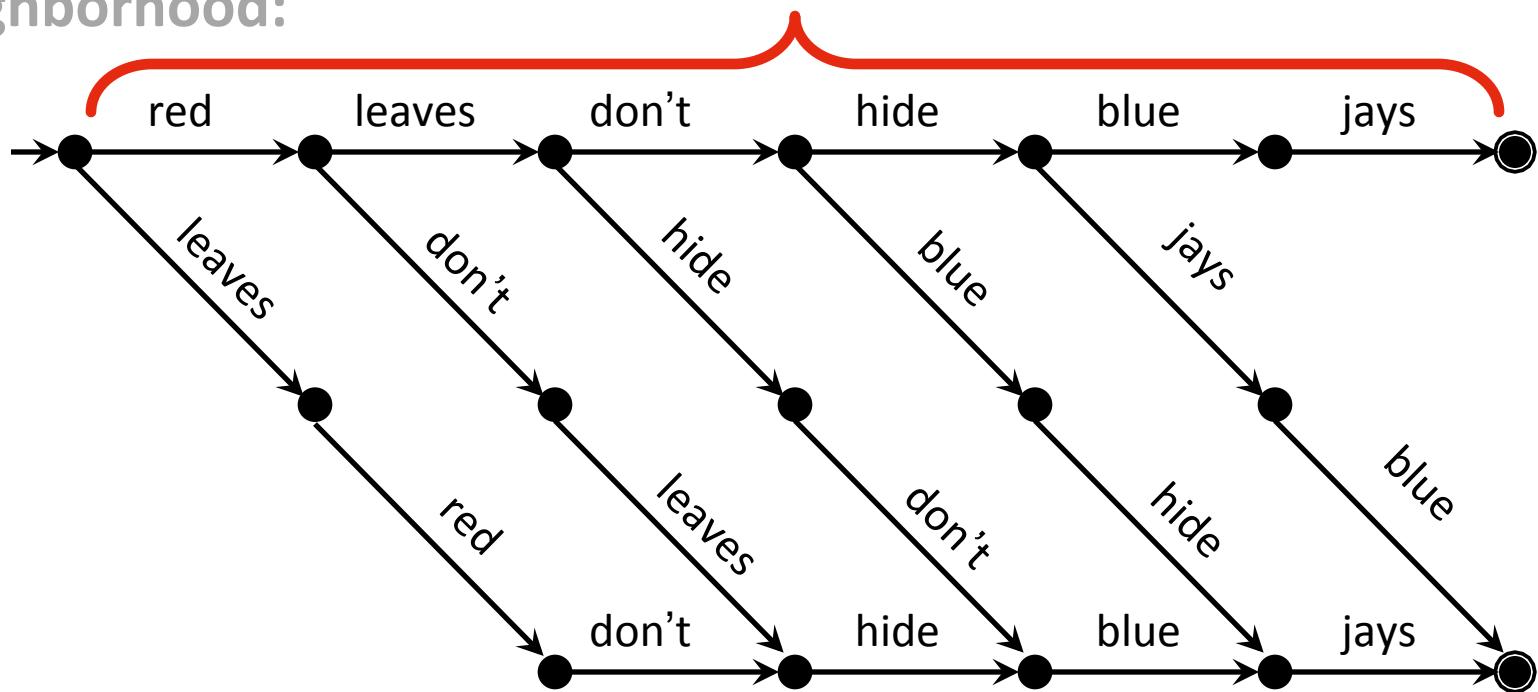
Smith & Eisner (2005)

# Transpose1 Neighborhood

Sentence: red leaves don't hide blue jays

neighborhood always contains original sentence

Neighborhood:

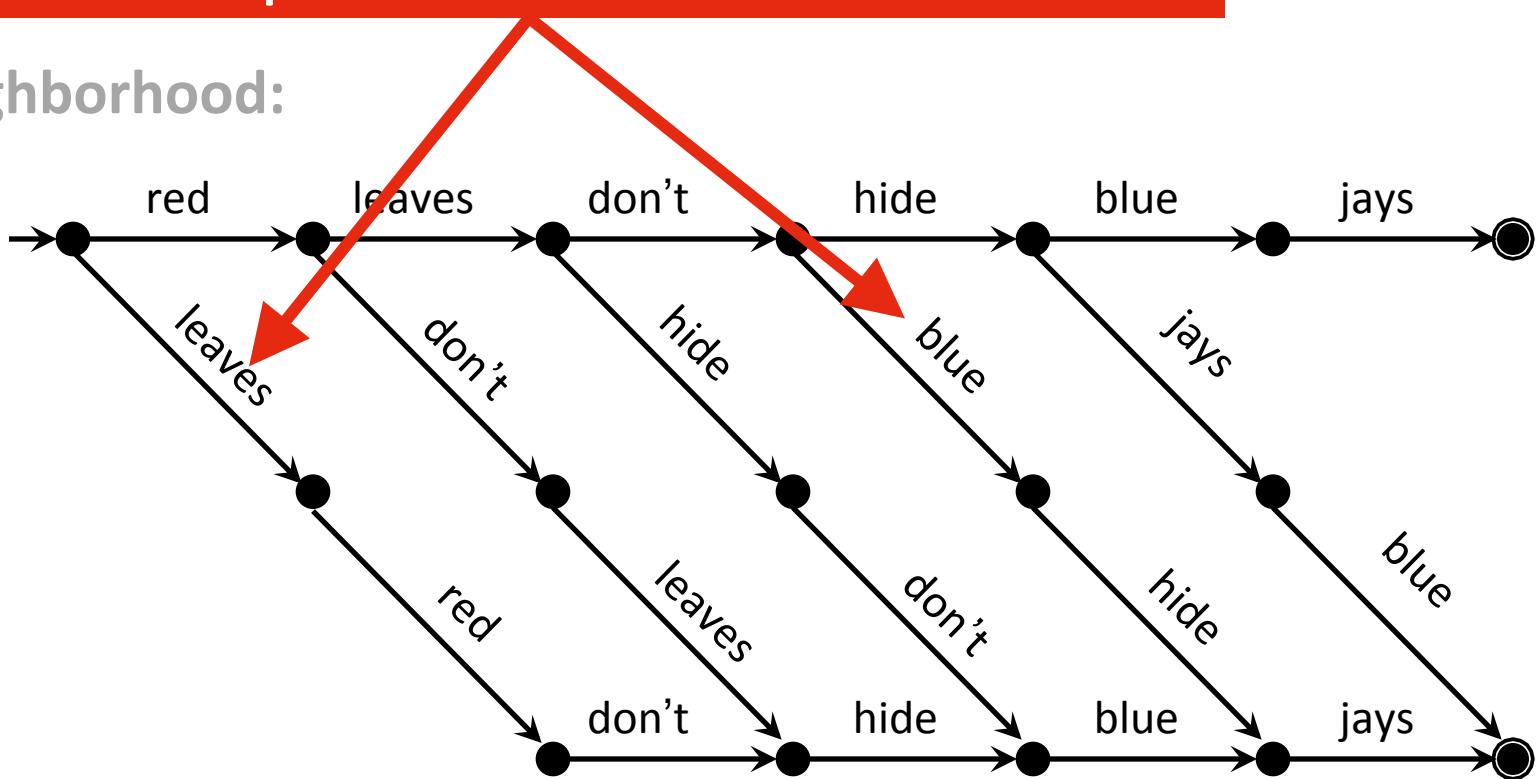


Smith & Eisner (2005)

# Transpose1 Neighborhood

some corruptions not as bad as others

Neighborhood:



Smith & Eisner (2005)

First modification:  
add **input cost function**  $\Delta(x, x')$

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$$\log \sum_{\mathbf{y}} \exp \left\{ \text{score}(\mathbf{x}^{(i)}, \mathbf{y}) \right\} - \log \sum_{\mathbf{x}' \in \mathcal{N}(\mathbf{x}^{(i)})} \sum_{\mathbf{y}'} \exp \left\{ \text{score}(\mathbf{x}', \mathbf{y}') + \underbrace{\alpha \Delta(\mathbf{x}^{(i)}, \mathbf{x}')}_{\text{measures difference between observed and corrupted sentences, } \alpha \text{ is weight}} \right\}$$

measures difference  
between observed and  
corrupted sentences,  
 $\alpha$  is weight

# Inspiration: Structured Large-Margin Learning

margin-rescaled structured hinge (Taskar et al., 2003):

$$\text{score}(\mathbf{x}^{(i)}, \mathbf{y}^{(i)}) - \max_{\mathbf{y}} \left( \text{score}(\mathbf{x}^{(i)}, \mathbf{y}) + \text{cost}(\mathbf{y}^{(i)}, \mathbf{y}) \right)$$

softmax-margin (Povey et al., 2008; Gimpel & Smith, 2010) :

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(soft)max-margin: cost compares two outputs

this talk: cost compares two **inputs**

# Input Cost Functions $\Delta(\mathbf{x}^{(i)}, \mathbf{x})$

## Match:

count unmatched bigrams in corrupted sentence

$$\sum_{j=1}^{|x|+1} \mathbb{I}\left[x_{j-1}x_j \notin \text{bigrams}(\mathbf{x}^{(i)})\right]$$

## Match LM:

weight by language model (negative) log-probability

$$\sum_{j=1}^{|x|+1} -\log \Pr(x_j | x_{j-1}) \mathbb{I}\left[x_{j-1}x_j \notin \text{bigrams}(\mathbf{x}^{(i)})\right]$$

# Experiments

Unsupervised part-of-speech tagging, 12 tags, no tag dictionaries

Evaluation: many-to-1 & 1-to-1 accuracy

5 languages from PASCAL 2012 shared task ([Gelling et al., 2012](#)):  
Danish, Dutch, Portuguese, Slovene, Swedish

# Neighborhoods

Transpose1 (Smith & Eisner, 2005)

Shuffle10:

original sentence + 10 random permutations

# Setup

Features:

tag-tag transitions

tag-word emissions

spelling features (Smith & Eisner, 2005)

tag-cluster emissions (from Brown clustering with {12,40} clusters)

LBFGS for 100 iterations, random initialization

L2 regularization with (untuned) coefficient 0.0001

	<b>input cost</b>	<b>many-to-1 accuracy</b>	<b>1-to-1 accuracy</b>
Shuffle10	None (CE baseline)	51.3	39.7
Transpose1	None (CE baseline)	61.8	47.2

avg. across 5 languages:  
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	input cost	many-to-1 accuracy	1-to-1 accuracy
	None (CE baseline)	51.3	39.7
	Match	53.3 (+2.0)	40.5 (+0.8)
Shuffle10	None (CE baseline)	61.8	47.2
Shuffle10	Match	63.1 (+1.3)	47.6 (+0.4)
Transpose1	None (CE baseline)	61.8	47.2
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Using language model probabilities helps

# EM and Contrastive Estimation

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Modification 2: Output Cost

# Contrastive Estimation:

$$\log \sum_{\mathbf{y}} \exp \left\{ \text{score}(\mathbf{x}^{(i)}, \mathbf{y}) \right\} - \log \sum_{\mathbf{x}' \in \mathcal{N}(\mathbf{x}^{(i)})} \sum_{\mathbf{y}'} \exp \left\{ \text{score}(\mathbf{x}', \mathbf{y}') \right\}$$

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we sum over all  $\mathbf{y}$ 's for each  $\mathbf{x}$  (observed or corrupted)

how can we encode intuitions about  $\mathbf{y}$ ?

## Second modification: adding an **output cost function** $\pi(\mathbf{y})$

$$\log \sum_{\mathbf{y}} \exp \left\{ \text{score}(\mathbf{x}^{(i)}, \mathbf{y}) - \beta \pi(\mathbf{y}) \right\} - \log \sum_{\mathbf{x}' \in \mathcal{N}(\mathbf{x}^{(i)})} \sum_{\mathbf{y}'} \exp \left\{ \text{score}(\mathbf{x}', \mathbf{y}') + \beta \pi(\mathbf{y}') \right\}$$

expresses preferences on  
outputs, regardless of input

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expresses preferences on outputs, regardless of input

similar to ``structural bias'' (Smith & Eisner, 2006), posterior regularization (Graça et al., 2010), and universal dependency rules (Naseem et al., 2010)

# Inspiration

Some objectives for *supervised* learning never need to score the true output:

ramp (Do et al., 2008):

$$\max_{\mathbf{y}} \text{score}(\mathbf{x}^{(i)}, \mathbf{y}) - \max_{\mathbf{y}'} \left( \text{score}(\mathbf{x}^{(i)}, \mathbf{y}') + \text{cost}(\mathbf{y}^{(i)}, \mathbf{y}') \right)$$



supervision  
used only in  
cost function

“Soft” ramp gain (Gimpel, 2012):

$$\log \sum_{\mathbf{y}} \exp \left\{ \text{score}(\mathbf{x}^{(i)}, \mathbf{y}) - \text{cost}(\mathbf{y}^{(i)}, \mathbf{y}) \right\} - \log \sum_{\mathbf{y}'} \exp \left\{ \text{score}(\mathbf{x}^{(i)}, \mathbf{y}') + \text{cost}(\mathbf{y}^{(i)}, \mathbf{y}') \right\}$$

CE with output cost function (this talk):

$$\log \sum_{\mathbf{y}} \exp \left\{ \text{score}(\mathbf{x}^{(i)}, \mathbf{y}) - \beta \pi(\mathbf{y}) \right\} - \log \sum_{\mathbf{x}' \in \mathcal{N}(\mathbf{x}^{(i)})} \sum_{\mathbf{y}'} \exp \left\{ \text{score}(\mathbf{x}', \mathbf{y}') + \beta \pi(\mathbf{y}') \right\}$$

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true y  
dropped  
from cost  
function

contrastive  
neighborhood used  
for denominator

# Universal Tag Priors

We counted tags in 11  
treebanks (for languages not  
used in our experiments)

$$\text{cost}(y) = \log \left( \frac{\max_{y'} \text{count}(y')}{\text{count}(y)} \right)$$

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$$\text{cost}(y) = \log \left( \frac{\max_{y'} \text{count}(y')}{\text{count}(y)} \right)$$

tag	count	cost
noun	2.3M	0
punctuation	1M	0.81
verb	1M	0.83
adposition	900K	0.95
adjective	700K	1.21
determiner	600K	1.33
pronoun	500K	1.62
conjunction	400K	1.68
adverb	300K	1.96
verb particle	179K	2.57
numeral	175K	2.59
X (“other”)	50K	3.83

<b>tag bigram</b>	<b>count</b>	<b>cost</b>
noun punctuation	500K	0
determiner noun	450K	1.04
noun noun	410K	2.09
...		
numeral adverb	1587	57.63
determiner conjunction	518	68.82
determiner particle	109	84.41

$$\text{cost}(\langle y_1, y_2 \rangle) = 10 \times \log \left( \frac{\max_{\langle y'_1, y'_2 \rangle} \text{count}(\langle y'_1, y'_2 \rangle)}{\text{count}(\langle y_1, y_2 \rangle)} \right)$$

# Results

	<b>many-to-1 accuracy</b>	<b>1-to-1 accuracy</b>
HMM, EM	50.9	34.2

accuracies averaged across 5 languages:  
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Brown Clustering	57.6	45.5
<a href="#">mkcls</a> ( <a href="#">Och, 1995</a> )	58.4	45.8

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Cost-Augmented Contrastive Estimation:

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### Cost-Augmented Contrastive Estimation:

Match LM	62.8	49.9
Universal	61.7	51.3

	<b>many-to-1 accuracy</b>	<b>1-to-1 accuracy</b>
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### Cost-Augmented Contrastive Estimation:

Match LM	62.8	49.9
Universal	61.7	51.3
Match LM + Universal	<b>64.3</b>	<b>51.7</b>

# Conclusions

- New learning criterion for weakly-supervised learning, generalizes contrastive estimation
- Cost functions allow modeler to direct learning in new ways
- Improves over strong POS tagging baselines

Thanks!

# Unsupervised Model Selection

1. Maximize CE objective on held-out data
2. Maximize log-likelihood of held-out data
  - using efficient estimator of [Bengio et al. \(2013\)](#)
3. Voting:
  - a. **naïve**: after making predictions with each model, return tags with most votes
  - b. **align**: solve weighted bipartite matching problems to align tag identifiers across runs, then do voting

# Comparing Model Selection Criteria

	cost	model selection	many-to-1 accuracy	1-to-1 accuracy
Shuffle10	Match LM	contrastive estimation	53.2 (+1.9)	40.2 (+0.5)
		log-likelihood	53.9 (+2.6)	41.6 (+1.9)
Transpose1	Match LM	contrastive estimation	62.2 (+0.4)	47.5 (+0.3)
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		log-likelihood	62.8 (+1.0)	49.9 (+2.7)

Log-likelihood works better than CE

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Posterior Regularization	60.9	50.1
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### Cost-Augmented Contrastive Estimation:

Match LM	62.8	49.9
Universal	61.7	51.3
Match LM + Universal (“naïve”)	60.6	51.4
Match LM + Universal (“align”)	<b>64.3</b>	<b>51.7</b>

Aligned voting works better than naïve voting