

# TTIC 31190: Natural Language Processing

Kevin Gimpel  
Spring 2018

Lecture 13:  
Brown Clustering;  
Syntax

# Project Proposal

- project proposal due Wednesday
- if you're still scrambling for project ideas, let me know and I can suggest a "default" project

# Midterm

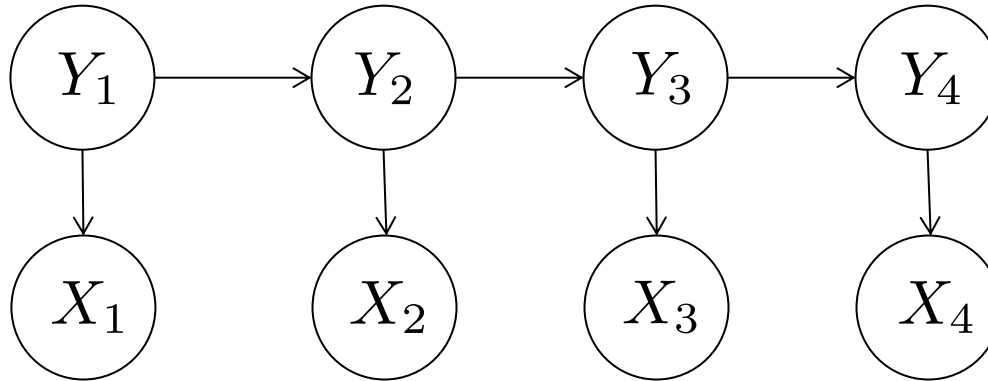
- midterm on Wednesday, May 16<sup>th</sup>
- you can bring notes
- we'll try to give you all the formulas/definitions you will need

# Roadmap

- words, morphology, lexical semantics
- text classification
- language modeling
- word embeddings
- recurrent/recursive/convolutional networks in NLP
- sequence labeling, HMMs, dynamic programming
- syntax and syntactic parsing
- semantics, compositionality, semantic parsing
- machine translation and other NLP tasks

# Graphical Model for an HMM

(for a sequence of length 4)

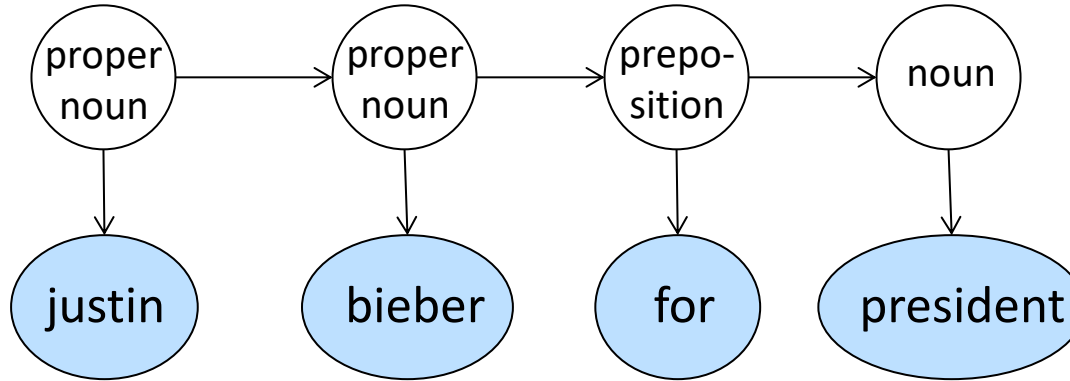


$$p_{\mathbf{w}}(\mathbf{x}, \mathbf{y}) = p_{\tau}(\langle /s \rangle | y_{|\mathbf{x}|}) \prod_{i=1}^{|\mathbf{x}|} p_{\tau}(y_i | y_{i-1}) p_{\eta}(x_i | y_i)$$

**transition parameters:**  $p_{\tau}(y_i | y_{i-1})$

**emission parameters:**  $p_{\eta}(x_i | y_i)$

# HMMs for Part-of-Speech Tagging



each  $y_i \in \mathcal{L}$  is a part-of-speech tag

so, label space is  $\mathcal{L} = \{\text{noun, verb, ...}\}$

transition parameters:  $p_{\tau}(y_i | y_{i-1})$

emission parameters:  $p_{\eta}(x_i | y_i)$

$$p_{\tau}(y | y') \leftarrow \frac{\text{count}(y' y)}{\text{count}(y')}$$

# Inference in HMMs

$$\text{classify}(\mathbf{x}, \mathbf{w}) = \underset{\mathbf{y}}{\operatorname{argmax}} p_{\mathbf{w}}(\mathbf{x}, \mathbf{y})$$

$$= \underset{\mathbf{y}}{\operatorname{argmax}} p_{\tau}(\langle / s \rangle \mid y_{|\mathbf{x}|}) \prod_{i=1}^{|\mathbf{x}|} p_{\tau}(y_i \mid y_{i-1}) p_{\eta}(x_i \mid y_i)$$

- output is a sequence; argmax requires iterating over an exponentially-large set
- **dynamic programming (DP)** can be used to solve such problems exactly
- for HMMs (& other sequence models):  
**Viterbi algorithm**

# Viterbi Algorithm for HMMs

- recursive equations + memoization:

**base case:**

returns probability of sequence starting with label  $y$  for first word



$$V(1, y) = p_{\eta}(x_1 | y) p_{\tau}(y | \langle s \rangle)$$

$$V(m, y) = \max_{y' \in \mathcal{L}} ( p_{\eta}(x_m | y) p_{\tau}(y | y') V(m - 1, y') )$$



**recursive case:**

computes probability of max-probability label sequence that ends with label  $y$  at position  $m$

**final value is in:**  $goal(\mathbf{x}) = \max_{y' \in \mathcal{L}} ( p_{\tau}(\langle /s \rangle | y') V(|\mathbf{x}|, y') )$



# Viterbi Algorithm for Sequence Models

(with tag bigram features)

$$V(1, y) = \text{score}(\mathbf{x}, \langle \langle s \rangle, y \rangle, 1, \mathbf{w})$$

$$V(m, y) = \max_{y' \in \mathcal{L}} (\text{score}(\mathbf{x}, \langle y', y \rangle, m, \mathbf{w}) + V(m - 1, y'))$$



score function for label bigram  $\langle y', y \rangle$   
ending at position  $m$  in  $\mathbf{x}$

could be anything!

linear model, feed-forward network,  
LSTM, etc.

# Viterbi Algorithm for Sequence Models

(with tag bigram features)

$$V(1, y) = \text{score}(\mathbf{x}, \langle \langle s \rangle, y \rangle, 1, \mathbf{w})$$

$$V(m, y) = \max_{y' \in \mathcal{L}} (\text{score}(\mathbf{x}, \langle y', y \rangle, m, \mathbf{w}) + V(m - 1, y'))$$



score function for label bigram  $\langle y', y \rangle$   
ending at position  $m$  in  $\mathbf{x}$

score for entire sequence:

$$\text{score}(\mathbf{x}, \mathbf{y}, \mathbf{w}) = \sum_i \text{score}(\mathbf{x}, \langle y_{i-1}, y_i \rangle, i, \mathbf{w})$$

(with appropriate handling of  $\langle s \rangle$  and  $\langle /s \rangle$ )

# Viterbi Algorithm for Sequence Models

(with tag bigram features)

## base case:

returns score of sequence starting with label  $y$  for word 1



$$V(1, y) = \text{score}(\mathbf{x}, \langle \langle s \rangle, y \rangle, 1, \mathbf{w})$$

$$V(m, y) = \max_{y' \in \mathcal{L}} (\text{score}(\mathbf{x}, \langle y', y \rangle, m, \mathbf{w}) + V(m - 1, y'))$$



## recursive case:

computes score of max-scoring label sequence that ends with label  $y$  at position  $m$

# Sequence Models with Tag Bigram Features

$$\text{score}(\mathbf{x}, \mathbf{y}, \mathbf{w}) = \sum_i \text{score}(\mathbf{x}, \langle y_{i-1}, y_i \rangle, i, \mathbf{w})$$

to recover HMM from this generalized score function, use the linear model features and weights we discussed last time

# Structured Models with Parts

$$\text{score}(\mathbf{x}, \mathbf{y}, \mathbf{w}) = \sum_i \text{score}(\mathbf{x}, \langle y_{i-1}, y_i \rangle, i, \mathbf{w})$$



$$\text{score}(\mathbf{x}, \mathbf{y}, \mathbf{w}) = \sum_{\langle \mathbf{x}_r, \mathbf{y}_r \rangle \in \text{parts}(\mathbf{x}, \mathbf{y})} \text{score}(\mathbf{x}_r, \mathbf{y}_r, \mathbf{w})$$

in general: structured prediction relies on decomposition of input/output into “parts”

score function defined on individual parts

size of each part (in terms of  $\mathbf{y}$ ) affects complexity of inference

# “Brown Clustering”

## Class-Based $n$ -gram Models of Natural Language

Peter F. Brown\*  
Peter V. deSouza\*  
Robert L. Mercer\*

Vincent J. Della Pietra\*  
Jenifer C. Lai\*

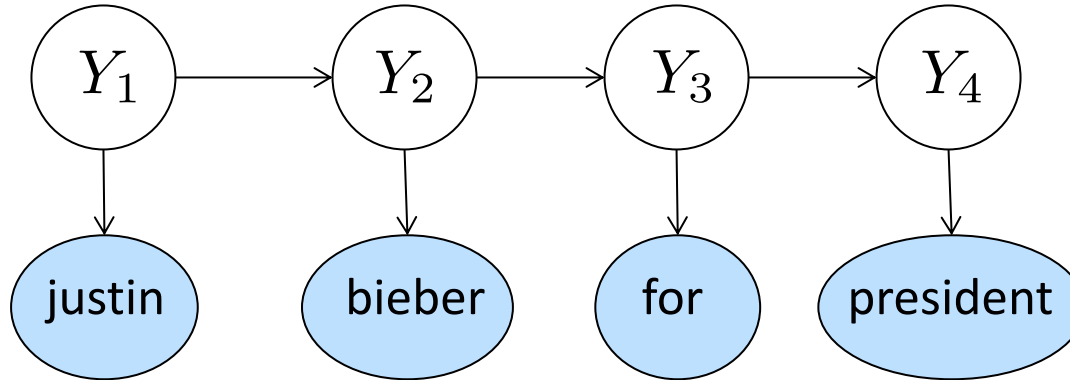
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Friday Monday Thursday Wednesday Tuesday Saturday Sunday weekends Sundays Saturdays  
June March July April January December October November September August  
people guys folks fellows CEOs chaps doubters commies unfortunates blokes  
down backwards ashore sideways southward northward overboard aloft downwards adrift  
water gas coal liquid acid sand carbon steam shale iron  
great big vast sudden mere sheer gigantic lifelong scant colossal

*Computational Linguistics, 1992*

# HMMs for Word Clustering

(Brown et al., 1992)



each  $y_i \in \mathcal{L}$  is a cluster ID

so, label space is  $\mathcal{L} = \{1, 2, \dots, 100\}$

## HMMs for POS Tagging

each  $y_i \in \mathcal{L}$  is a POS tag  
so, label space is

$$\mathcal{L} = \{\text{noun, verb, ...}\}$$

**transition parameters:**

$$p_{\tau}(\text{verb} \mid \text{noun})$$

$$p_{\tau}(\text{noun} \mid \text{noun})$$

...

**emission parameters:**

$$p_{\eta}(\textit{for} \mid \text{noun})$$

$$p_{\eta}(\textit{walk} \mid \text{noun})$$

...

## HMMs for Word Clustering

each  $y_i \in \mathcal{L}$  is a cluster ID  
so, label space is

$$\mathcal{L} = \{1, 2, \dots, 100\}$$

**transition parameters:**

$$p_{\tau}(1 \mid 17)$$

$$p_{\tau}(2 \mid 17)$$

...

**emission parameters:**

$$p_{\eta}(\textit{for} \mid 17)$$

$$p_{\eta}(\textit{walk} \mid 17)$$

...



# HMMs for Word Clustering


(Brown et al., 1992)

- given a set of sentences, how should we learn the parameters of our model?
- how about we use maximum likelihood estimation, e.g.:

$$\operatorname{argmax}_w \sum_{i=1}^N \log p_w(\mathbf{x}^{(i)}, \mathbf{y}^{(i)})$$


- problem: we don't have any  $\mathbf{y}^{(i)}$ 's!
- we only have a set of **unlabeled** sentences:  $\{\mathbf{x}^{(i)}\}_{i=1}^N$

- we want to maximize likelihood, but:
  - our HMM defines  $p_{\mathbf{w}}(\mathbf{x}^{(i)}, \mathbf{y}^{(i)})$
  - our data only contains  $\mathbf{x}$
- solution: marginalize out  $\mathbf{y}$
- this idea underlies much of unsupervised learning

$$\operatorname{argmax}_{\mathbf{w}} \sum_{i=1}^N \log p_{\mathbf{w}}(\mathbf{x}^{(i)}, \mathbf{y}^{(i)})$$


$$\operatorname{argmax}_{\mathbf{w}} \sum_{i=1}^N \log \sum_{\mathbf{y}} p_{\mathbf{w}}(\mathbf{x}^{(i)}, \mathbf{y})$$

- we want to maximize likelihood, but:
  - our HMM defines  $p_w(\mathbf{x}^{(i)}, \mathbf{y}^{(i)})$
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- solution: marginalize out  $\mathbf{y}$
- this idea underlies much of unsupervised learning

$$\operatorname{argmax}_w \sum_{i=1}^N \log \sum_{\mathbf{y}} p_w(\mathbf{x}^{(i)}, \mathbf{y})$$

a sum over an exponentially-large set

- learning requires sum over exponentially-large set
  - all possible clusterings of the words

$$\operatorname{argmax}_w \sum_{i=1}^N \log \sum_{\mathbf{y}} p_w(\mathbf{x}^{(i)}, \mathbf{y})$$

- for HMMs, we can compute this sum in polynomial time using dynamic programming
- however, Brown clustering uses simplifying assumption: **each word is in exactly one cluster**
- the summation above becomes trivial to compute!

# One Cluster Per Word Assumption

$$\operatorname{argmax}_w \sum_{i=1}^N \log \sum_{\mathbf{y}} p_w(\mathbf{x}^{(i)}, \mathbf{y})$$

- summation becomes trivial, so we can easily compute the log-likelihood of any given model
- but how should we do learning?
  - gradient-based optimization is tricky due to the constraints
  - and it's too expensive to iterate through all possible clusterings and compute their likelihoods

# Algorithm for Brown Clustering

greedy algorithm:

- initialize each word as its own cluster
- greedily merge clusters to improve data likelihood

we induced 1000 Brown clusters from 56 million English tweets (1 billion words)

only words that appeared at least 40 times

(Owoputi, O'Connor, Dyer, Gimpel, Schneider, and Smith, 2013)

# Example Cluster

missed loved hated misread admired  
underestimated resisted adored disliked  
regretted missd fancied luvd preferred luvd  
overdid mistyped misd missed looooved  
misjudged lovedd loooved loathed lurves lovd



# Example Cluster

missed loved hated misread admired  
underestimated resisted adored disliked  
regretted **missd** fancied luvd preferred luvd  
overdid mistyped **misd** **misssed** looooved  
misjudged lovedd lo **oved** loathed lurves lovd

spelling  
variation

# “really”

really rly realy genuinely rily reallly reallly  
really rele realli relly realllly reli reali sholl rily  
reallyyy reee really reallllly reaally reee really rili  
reaaally reaaaally reallyyyy rilly realllllly  
reeeee really reeally shol realllyyy reely relle  
reaaaaally shole really2 reallyyyyy \_really\_  
reallllllly reaaly realllyy reallii realt genuinly relli  
realllyyyy reeeee really weally reaaally realllyyy  
reallllllly reaally realyy /really/ reaaaaaally reallu  
reaaaally reeaally rreally reallyreally eally reeeaaally reeeaaally  
reaally reallyyyyyy –really- reallyreallyreally rilli realllyyyy relaly  
realllyy really-really r3ally reeli reallie realllyyy rli reallllllly  
reaaaly reeeee really

# “SO”

S00 S000 S0000 S00000 S000000 S0000000  
S00000000 S000000000 S0000000000  
S00000000000 S000000000000  
S0000000000000 S0S0 S000000000000000  
S000000000000000 S00000000000000000  
S0S0S0 superrr S000000000000000000 S000  
S000 superrrr S00 S0000000000000000000  
S0S0S0S0 S000000000000000000000 S00 SSS000  
S0000000000000000000000 #too S00 S0000 S00

# Food-Related Adjectives

hot fried peanut homemade grilled spicy soy cheesy coconut  
veggie roasted leftover blueberry icy dunkin mashed rotten  
mellow boiling crispy peppermint fruity toasted crunchy  
scrambled creamy boiled chunky funnel soggy clam steamed  
cajun steaming chewy steamy nacho mince reese's shredded  
salted glazed spiced venti pickled powdered butternut miso beet  
sizzling

# “going to”

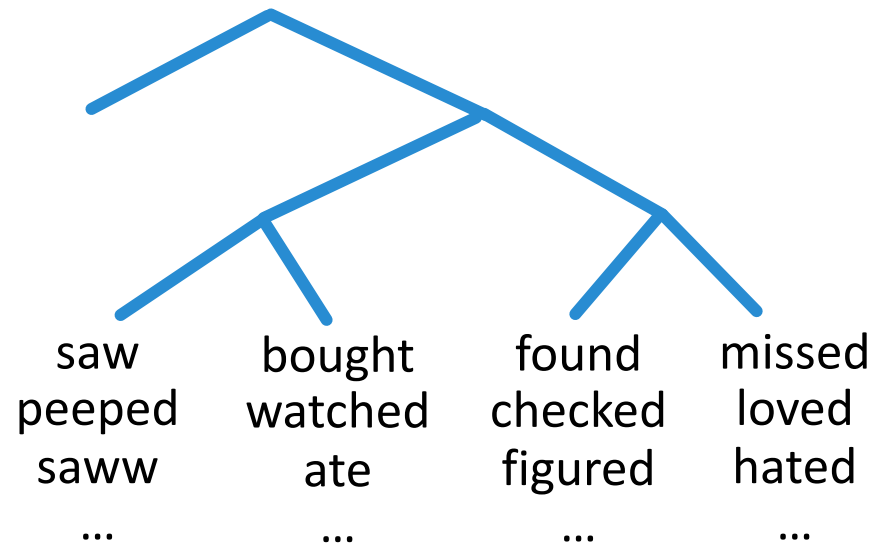
gonna gunna gona gna guna gnna ganna qonna  
gonnna gana qunna gone goona gonnaa g0nna  
goina gonnah goingto gunnah gonaa gonan  
gunnna going2 gonnnnagunnaa gonny gunaa  
quna goonna qona gonns goinna gonnae qnna  
gonnaaa gnaa

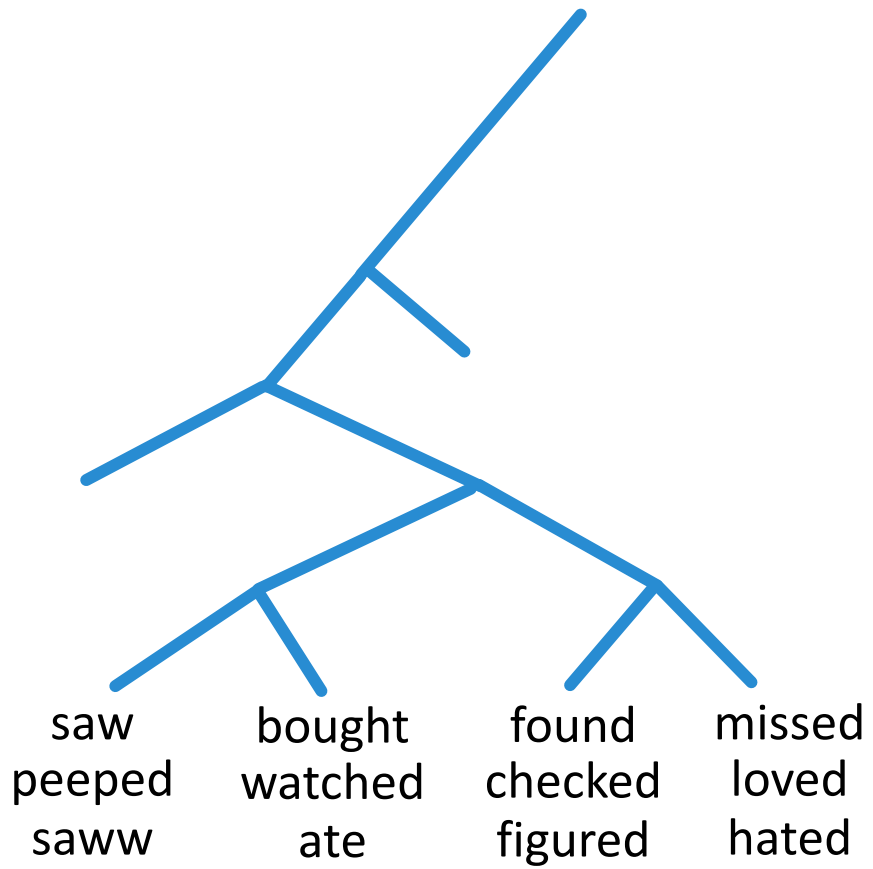
# Adjective Intensifiers/Qualifiers

kinda hella sorta hecka kindof kindaa kinna hella propa  
helluh kindda justa #slick helllla hela jii sortof hellaa  
kida wiggity helllla hekka hellah kindaaa hellaaa kindah  
knda kind-of slicc wiggidy hellllla jih jye kinnda odhee  
kiinda heka sorda ohde kind've kidna baree rle hellaaaa  
jussa

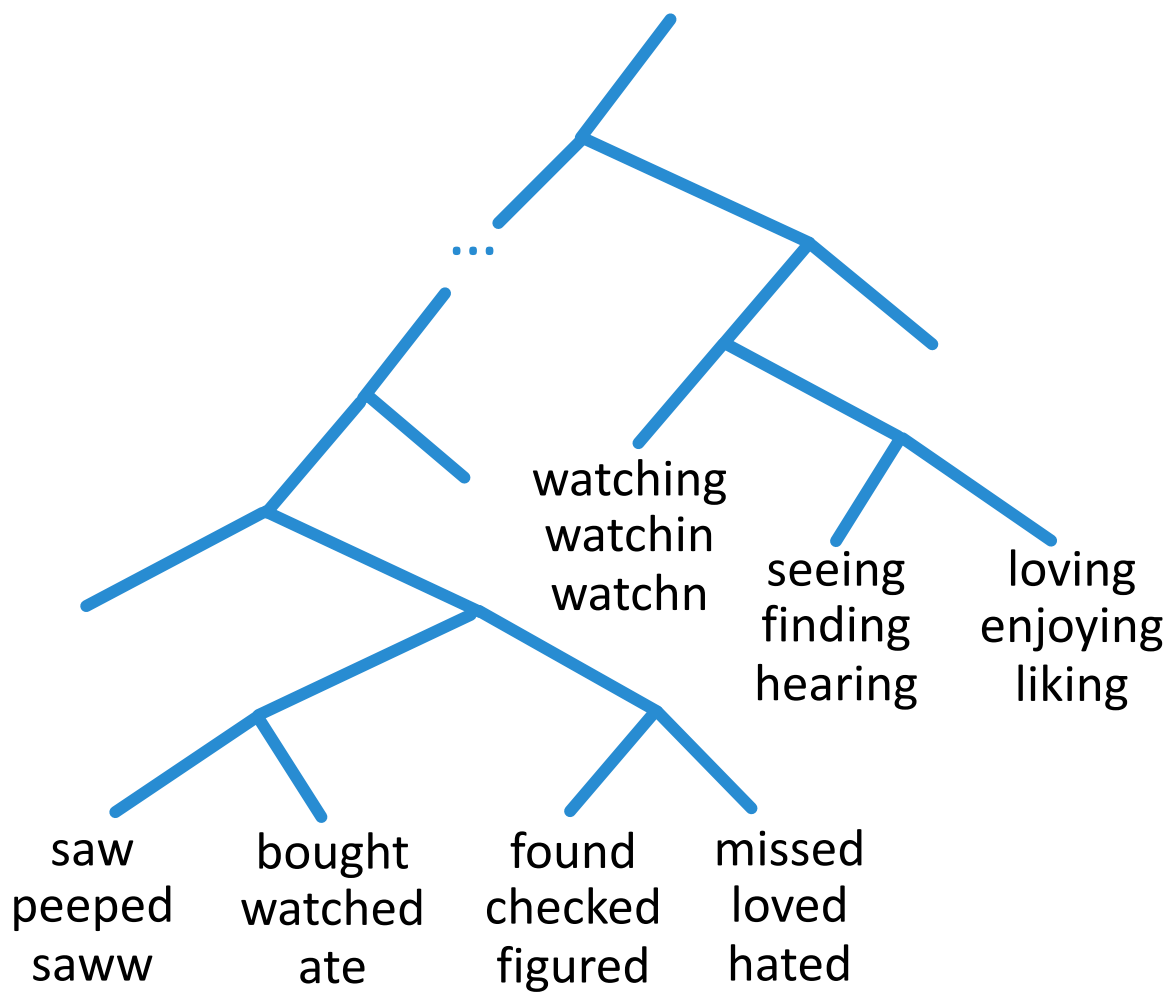
# Hierarchical Clustering from Brown Clusters

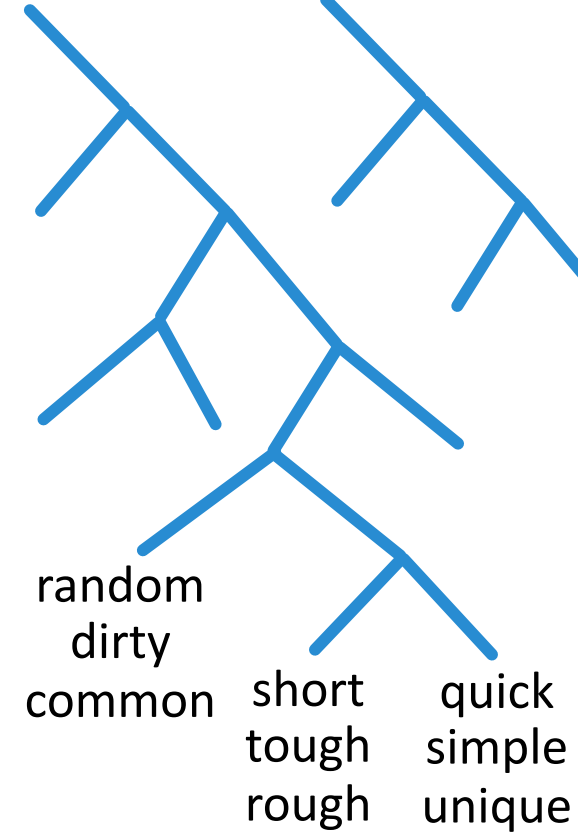
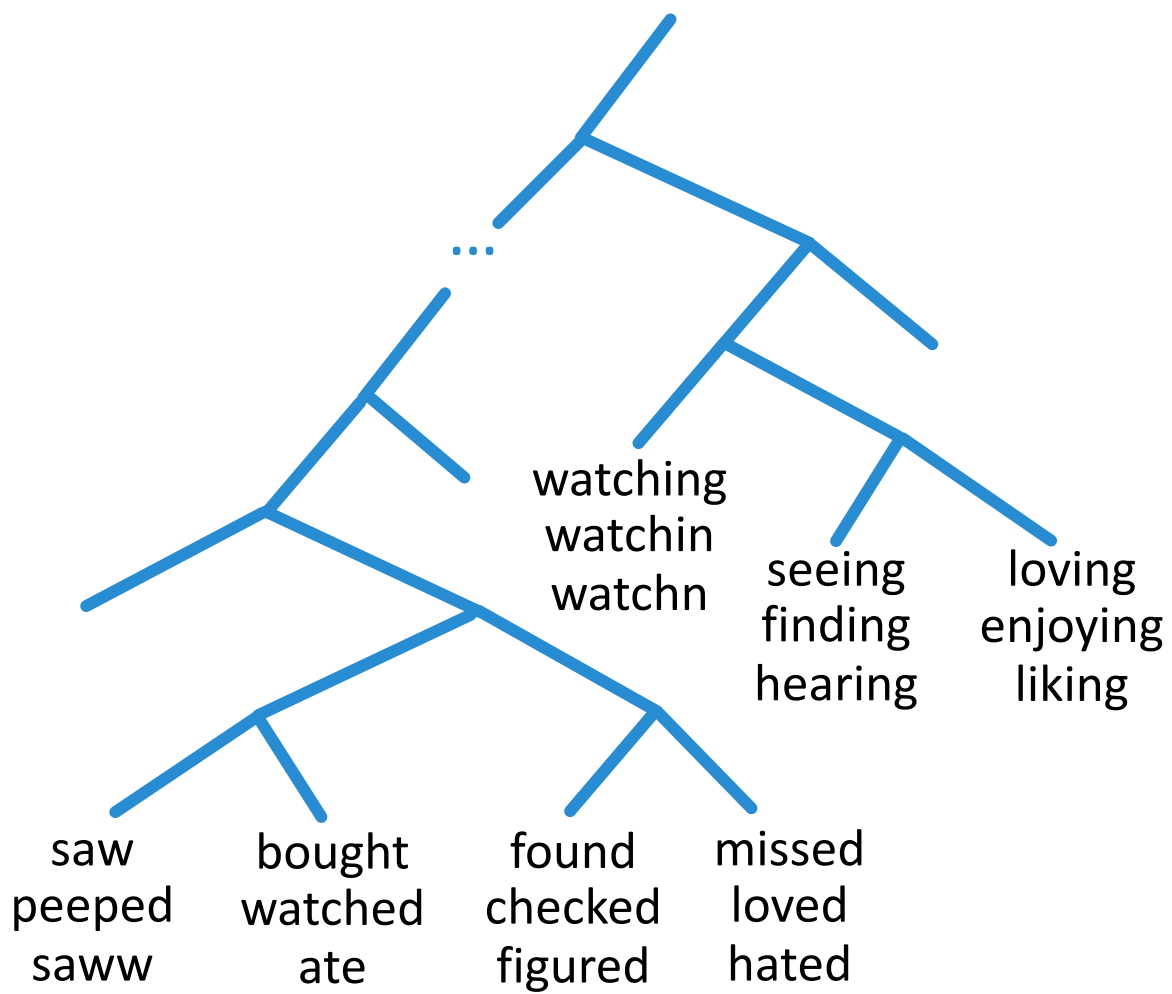
- we have a sequence of clustering decisions
- we can use the order in which clusters are merged to create a **hierarchical clustering**
  - build a binary tree to represent the merges
  - word similarity is captured by distance in the tree

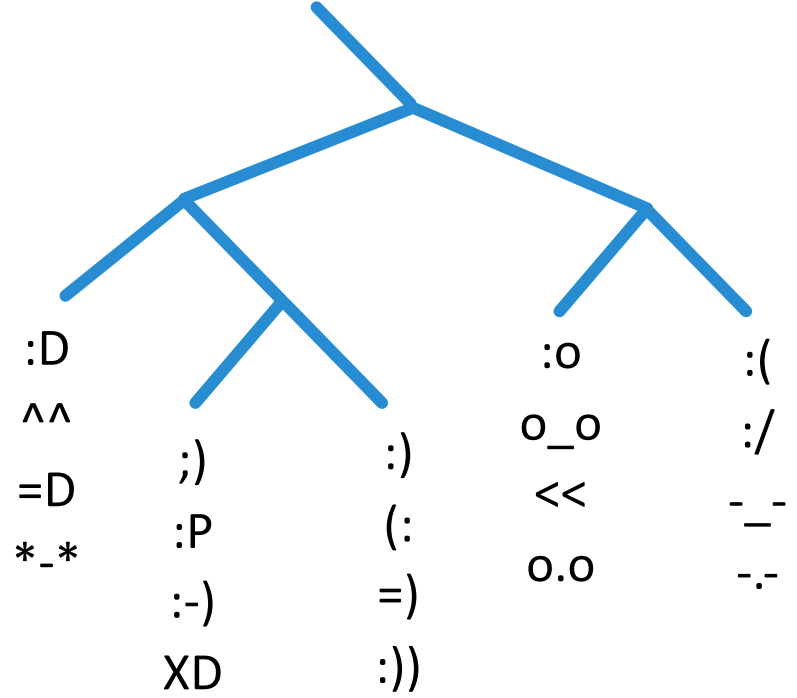
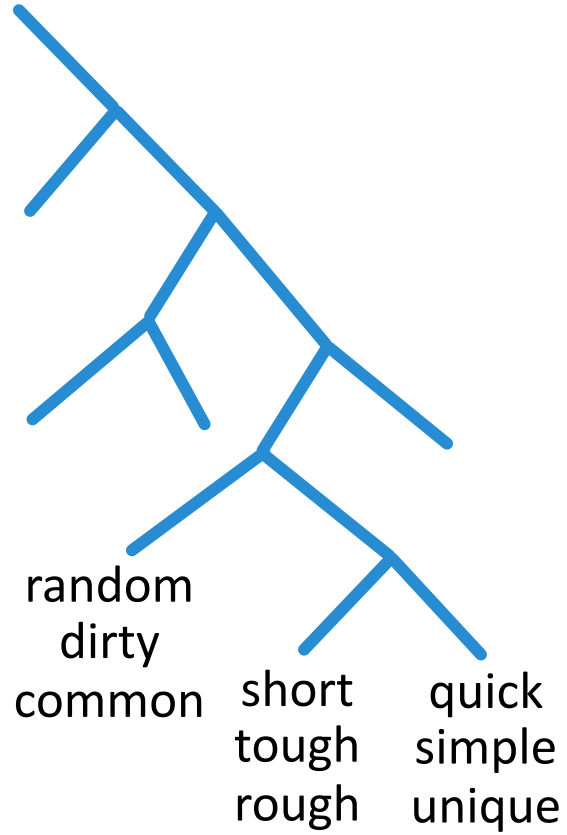




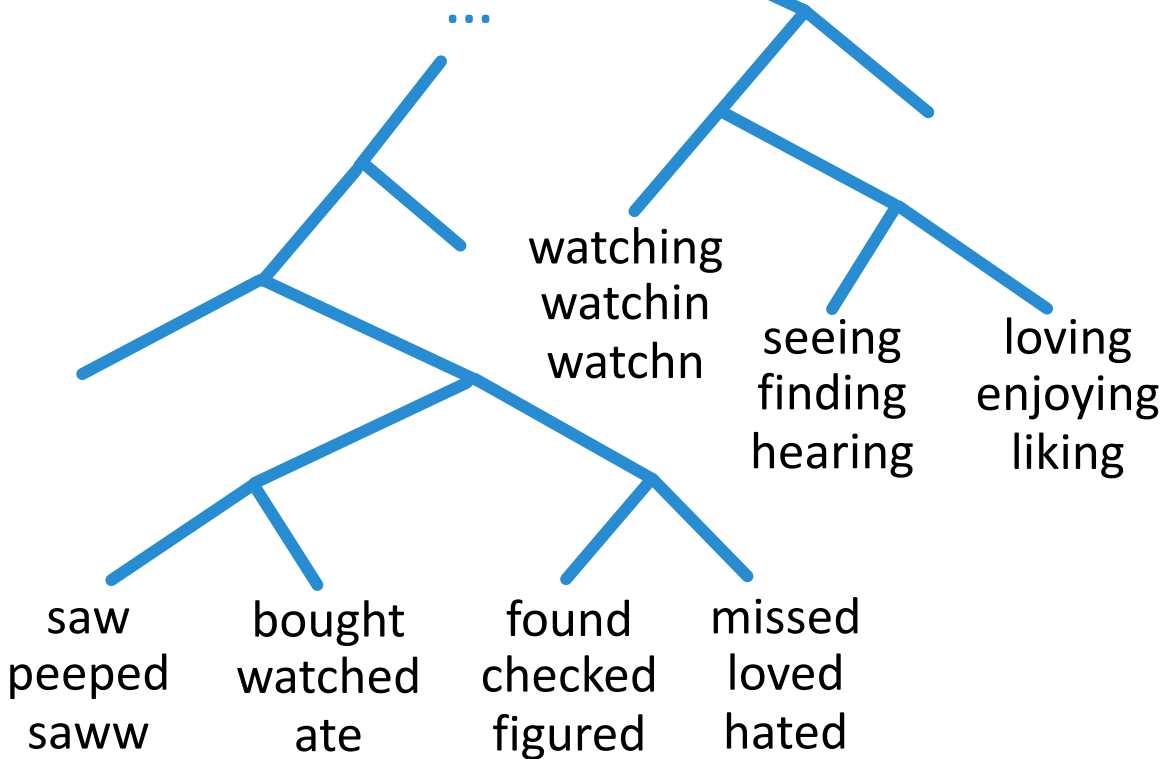




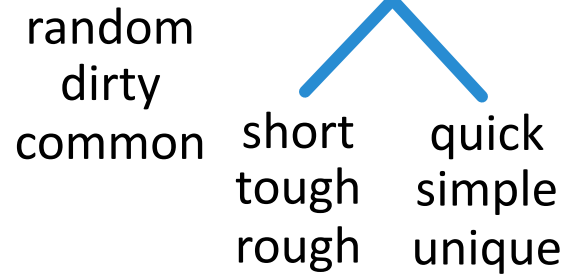


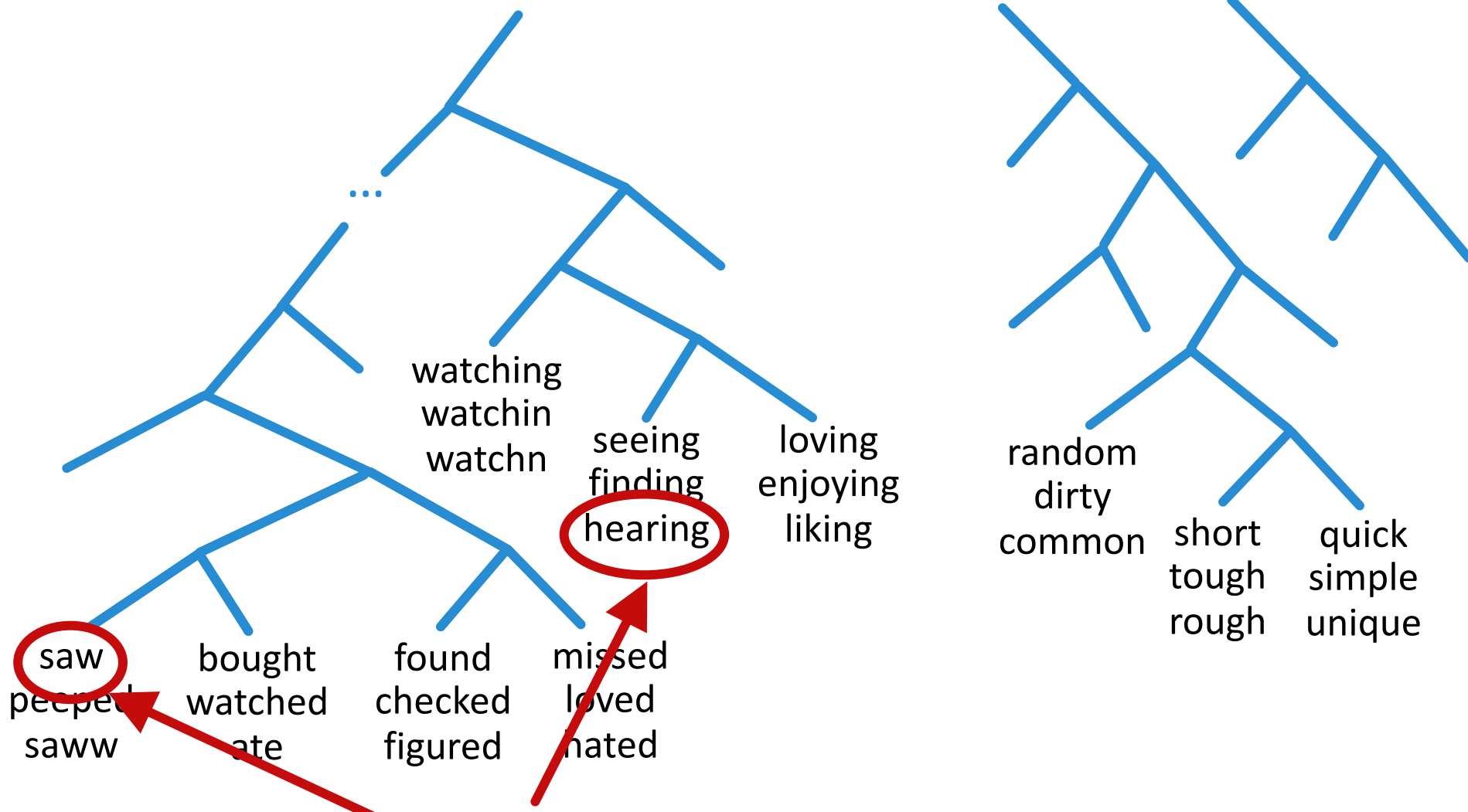


verbs?

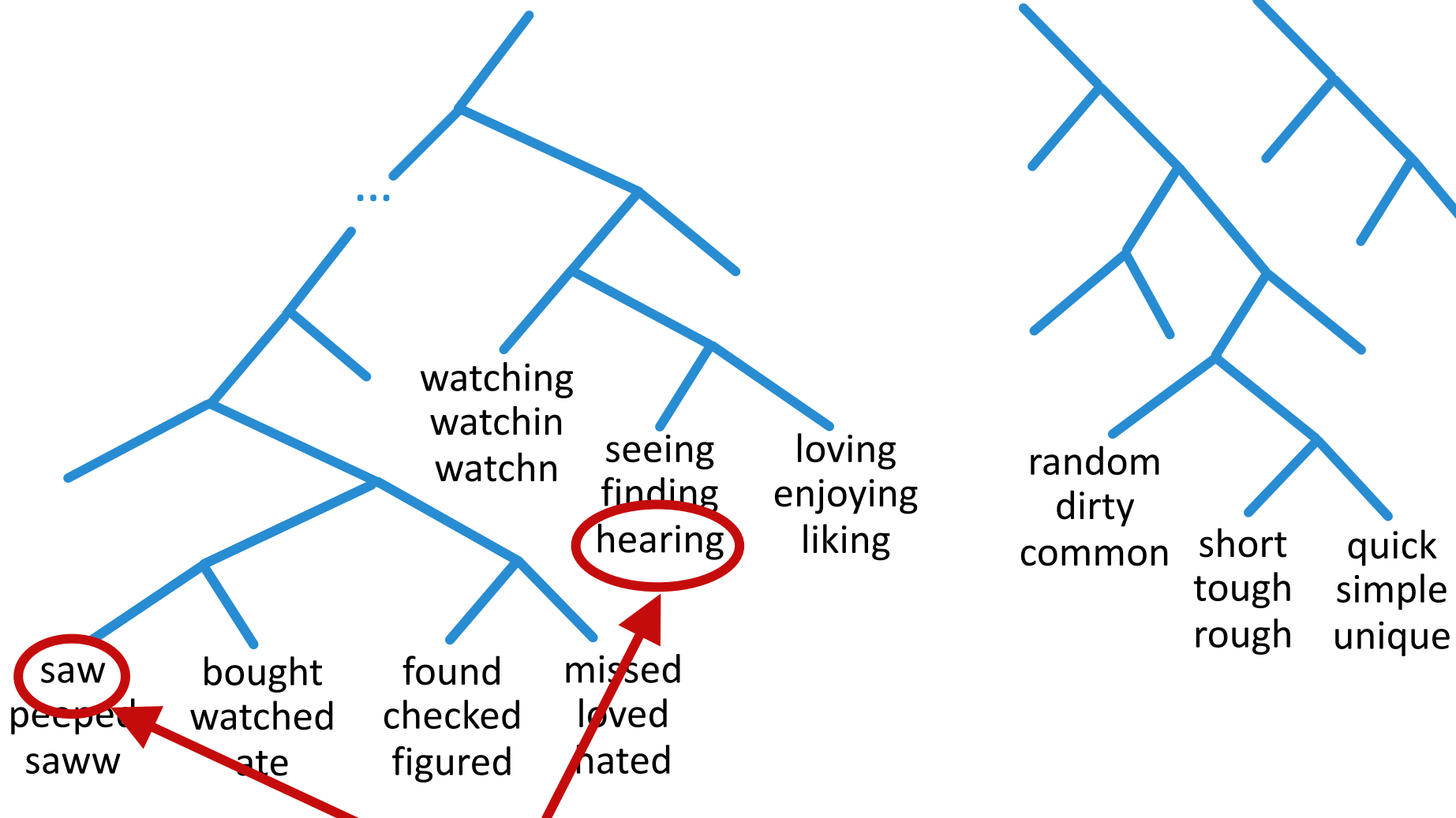


adjectives?





could be verbs or nouns, but  
 Brown clustering uses one-cluster-per-word constraint

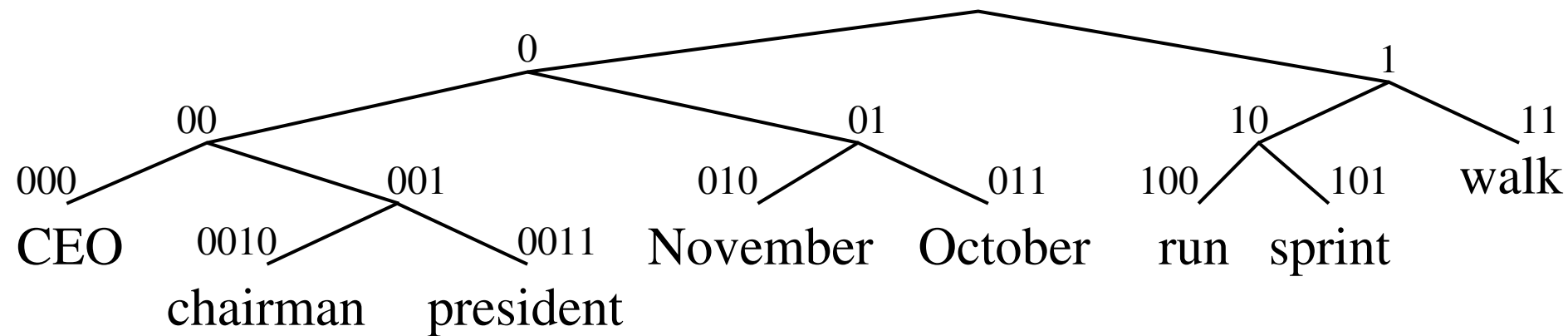


could be verbs or nouns, but one-cluster-per-word

even so, Brown clusters are good unsupervised POS tags!

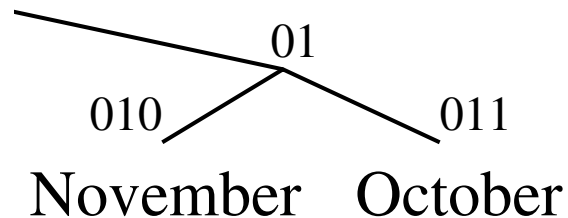
# Brown Clusters as Vectors

- cluster merging represented by a binary tree
- each word can be represented by its binary string = path from root to leaf
- each intermediate node is a cluster
- *chairman* is 0010, “months” = 01, verbs = 1:



# Brown Clusters for Downstream Tasks

- even with one-cluster-per-word constraint, Brown clusters are really useful for syntactic tasks (tagging, parsing, etc.)
- also helps to use different granularities of the hierarchical clustering:
  - define features based on prefixes of binary strings:



- November and October will share feature that looks at “length-2 prefix of binary string”



# Roadmap






- words, morphology, lexical semantics
- text classification
- language modeling
- word embeddings
- recurrent/recursive/convolutional networks in NLP
- sequence labeling, HMMs, dynamic programming
- **syntax and syntactic parsing**
- semantics, compositionality, semantic parsing
- machine translation and other NLP tasks

# What is Syntax?

- rules, principles, processes that govern sentence structure of a language
- can differ widely among languages
- but every language has systematic structural principles

# Subject, Verb, Object

- syntax determines the ordering of these three objects in a sentence

Word order	English equivalent	Proportion of languages	Example languages
SOV	"She him loves."	45% 	Hindi, Latin, Japanese, Marathi
SVO	"She loves him."	42% 	English, Hausa, Mandarin, Russian
VSO	"Loves she him."	9% 	Biblical Hebrew, Irish, Filipino, Tuareg
VOS	"Loves him she."	3% 	Malagasy, Baure
OVS	"Him loves she."	1% 	Apalaí, Hixkaryana
OSV	"Him she loves."	0%	Warao

Frequency distribution of word order in languages surveyed by Russell S. Tomlin in 1980s<sup>[1][2]</sup> ( V • T • E )

# Yodish

- often (though certainly not always) Yoda uses object-subject-verb order



*“Powerful you have become.  
The dark side I sense in you.”*

# Grammars

- we will use **grammar** to denote a formal object that represents the rules/principles/processes that determine sentence structure

# phrase structure / constituent grammar

- focuses on the **constituent** relation
- informally: “sentences have hierarchical structure”
- a sentence is made up of two pieces:
  - subject, typically a **noun phrase (NP)**
  - predicate, typically a **verb phrase (VP)**
- NPs and VPs are in turn made of up of pieces:
  - old books = (old + books)
  - the old books = (the + (old + books))
  - walked to the park = (walked + (to + (the + park)))
- each parenthesized phrase is a **constituent** in the **constituent parse**

# Bracketing

- constituent parse = **bracketing** (that represents the hierarchical structure)

- e.g., sentence:

*the man walked to the park*

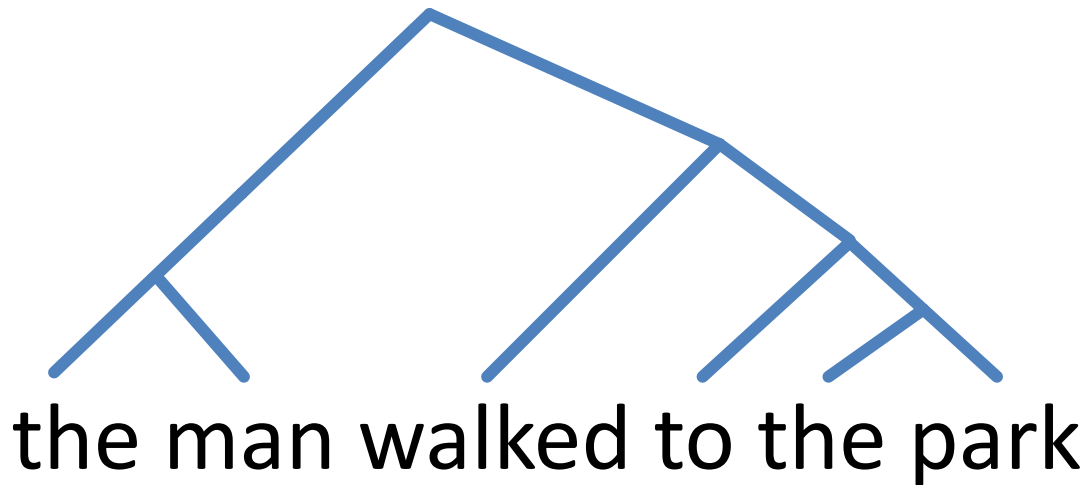
- bracketing:

*((the man) (walked (to (the park))))*

# Bracketing → Tree

((the man) (walked (to (the park))))

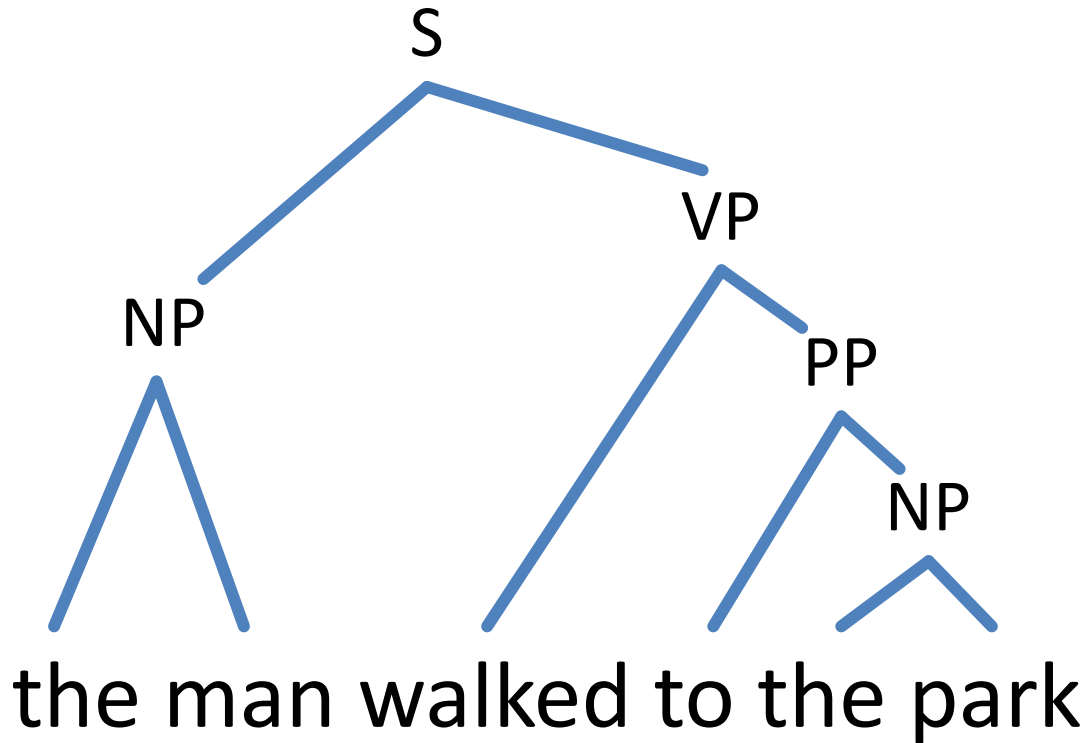
we often draw the bracketing as a tree:





# Labeled Bracketings/Trees

(S (NP the man) (VP walked (PP to (NP the park))))



Key:

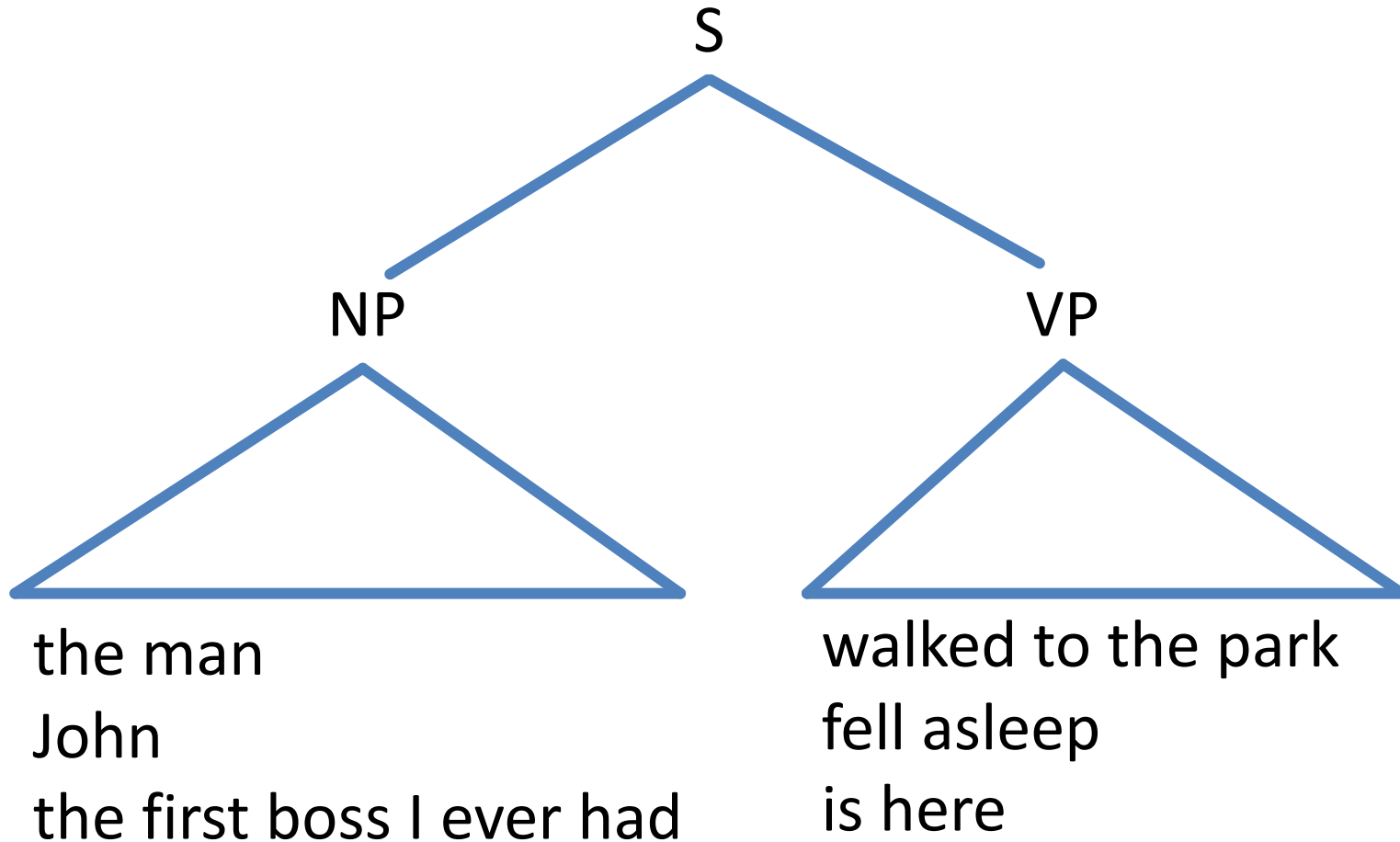
S = sentence

NP = noun phrase

VP = verb phrase

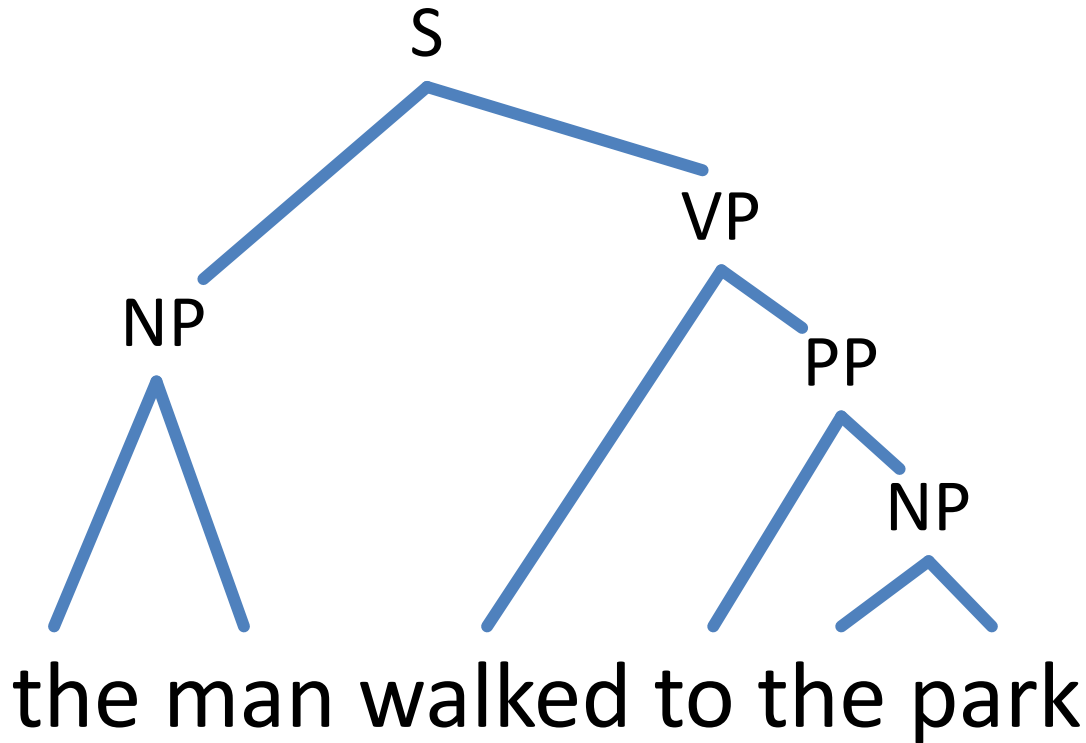
PP = prepositional phrase

# Labels → Substitutability



# Labeled Bracketings/Trees

(S (NP the man) (VP walked (PP to (NP the park))))



Key:

S = sentence

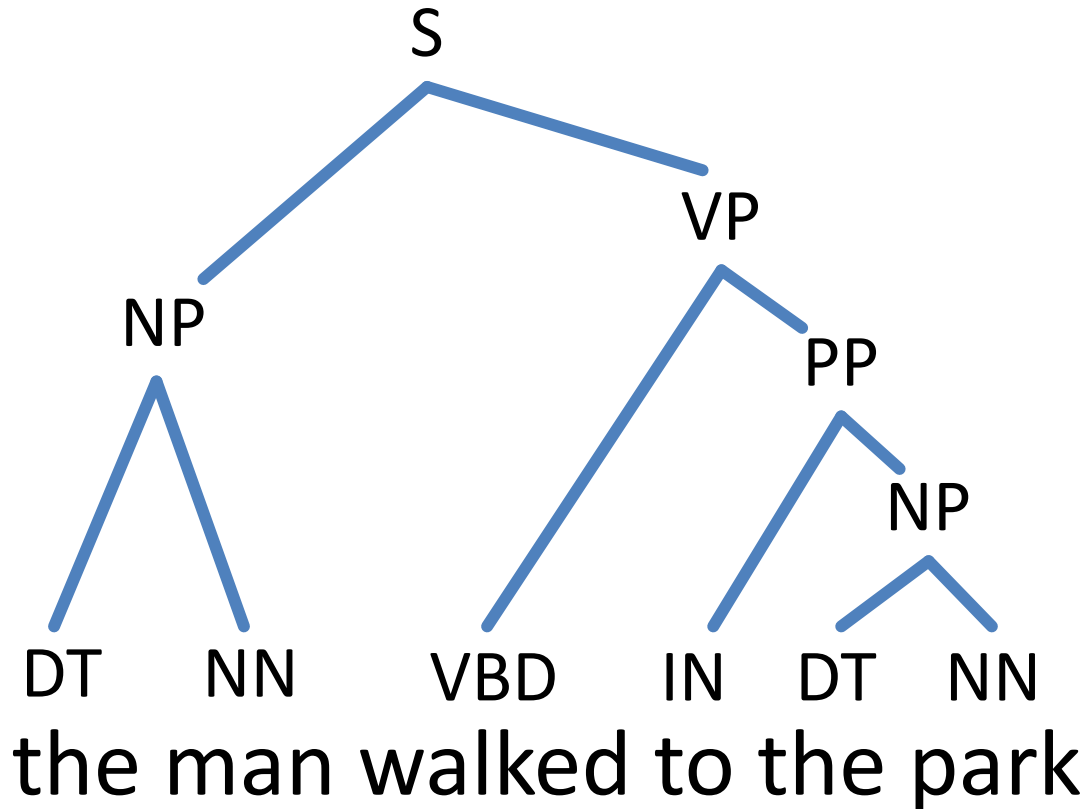
NP = noun phrase

VP = verb phrase

PP = prepositional phrase

# Labeled Bracketings/Trees

(S (NP the man) (VP walked (PP to (NP the park))))



Key:

S = sentence

NP = noun phrase

VP = verb phrase

PP = prepositional phrase

DT = determiner

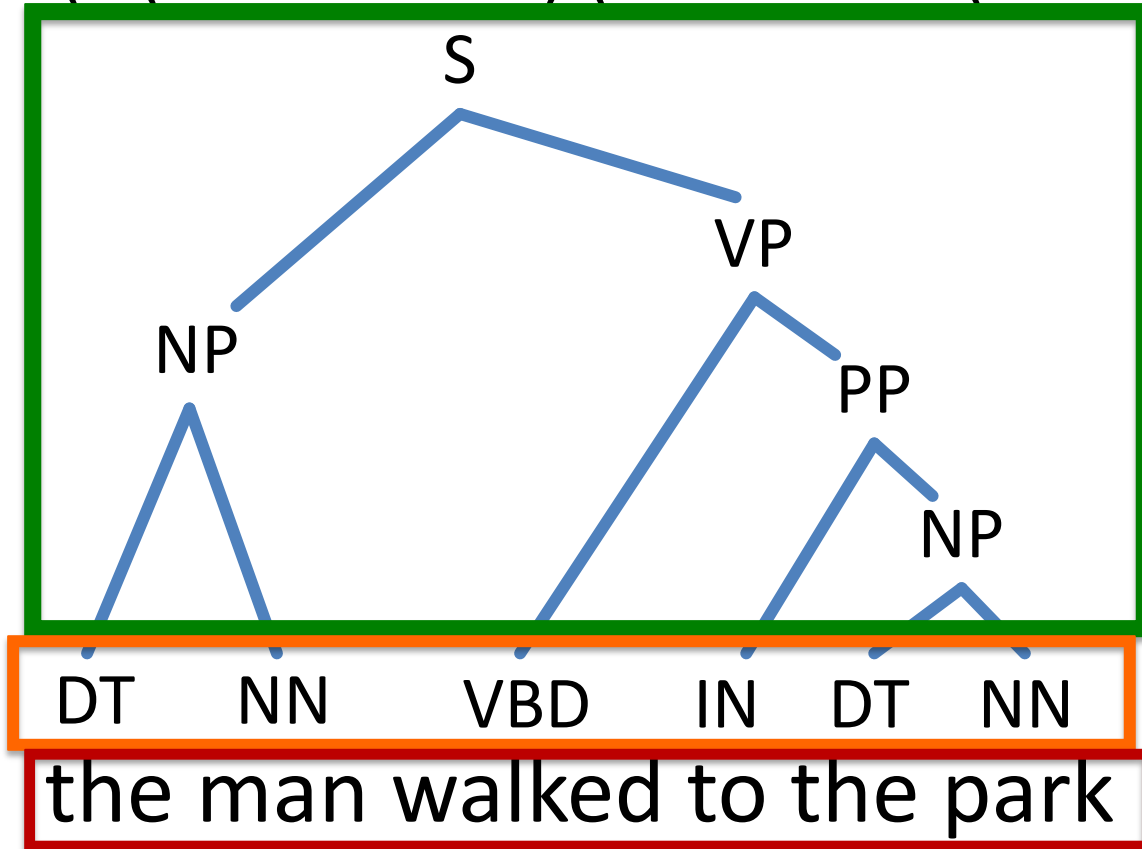
NN = noun

VBD = verb (past tense)

IN = preposition

# Labeled Bracketings/Trees

(S (NP the man) (VP walked (PP to (NP the park))))



**nonterminals**

**preterminals**

**terminals**

Penn  
Treebank  
tag set

Tag	Description	Example	Tag	Description	Example
CC	coordin. conjunction	<i>and, but, or</i>	SYM	symbol	<i>+, %, &amp;</i>
CD	cardinal number	<i>one, two</i>	TO	“to”	<i>to</i>
DT	determiner	<i>a, the</i>	UH	interjection	<i>ah, oops</i>
EX	existential ‘there’	<i>there</i>	VB	verb base form	<i>eat</i>
FW	foreign word	<i>mea culpa</i>	VBD	verb past tense	<i>ate</i>
IN	preposition/sub-conj	<i>of, in, by</i>	VBG	verb gerund	<i>eating</i>
JJ	adjective	<i>yellow</i>	VBN	verb past participle	<i>eaten</i>
JJR	adj., comparative	<i>bigger</i>	VBP	verb non-3sg pres	<i>eat</i>
JJS	adj., superlative	<i>wildest</i>	VBZ	verb 3sg pres	<i>eats</i>
LS	list item marker	<i>1, 2, One</i>	WDT	wh-determiner	<i>which, that</i>
MD	modal	<i>can, should</i>	WP	wh-pronoun	<i>what, who</i>
NN	noun, sing. or mass	<i>llama</i>	WP\$	possessive wh-	<i>whose</i>
NNS	noun, plural	<i>llamas</i>	WRB	wh-adverb	<i>how, where</i>
NNP	proper noun, sing.	<i>IBM</i>	\$	dollar sign	<i>\$</i>
NNPS	proper noun, plural	<i>Carolinas</i>	#	pound sign	<i>#</i>
PDT	predeterminer	<i>all, both</i>	“	left quote	<i>‘ or “</i>
POS	possessive ending	<i>'s</i>	”	right quote	<i>’ or ”</i>
PRP	personal pronoun	<i>I, you, he</i>	(	left parenthesis	<i>[, (, {, &lt;</i>
PRP\$	possessive pronoun	<i>your, one’s</i>	)	right parenthesis	<i>], ), }, &gt;</i>
RB	adverb	<i>quickly, never</i>	,	comma	<i>,</i>
RBR	adverb, comparative	<i>faster</i>	.	sentence-final punc	<i>. ! ?</i>
RBS	adverb, superlative	<i>fastest</i>	:	mid-sentence punc	<i>: ; ... --</i>
RP	particle	<i>up, off</i>			

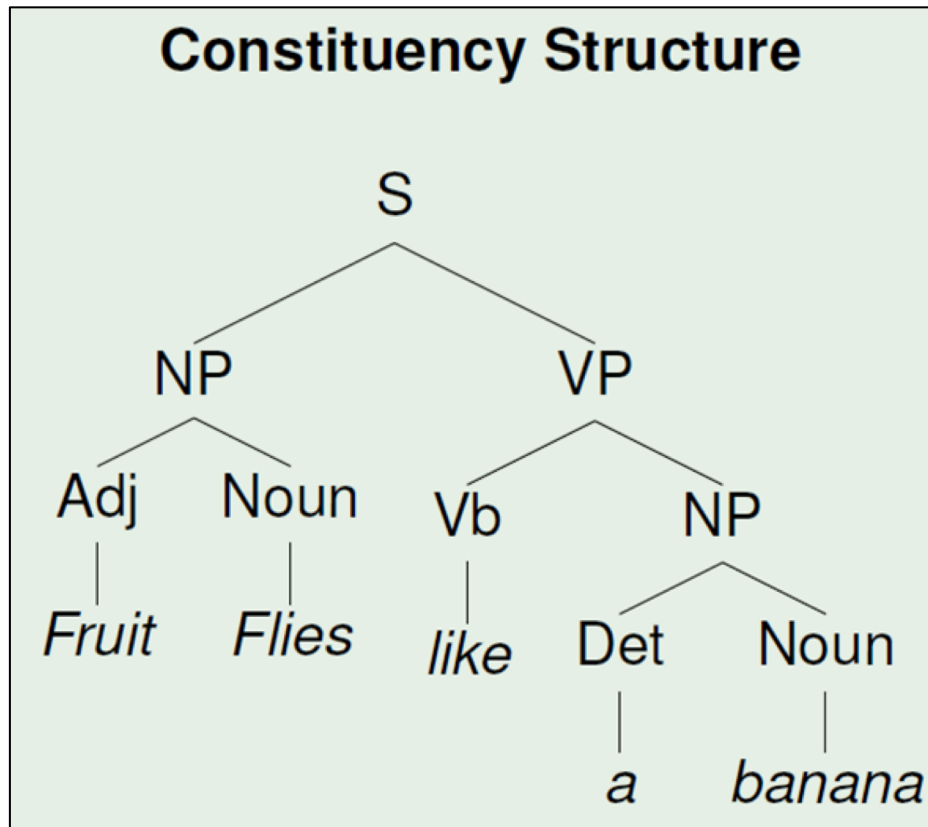
# Penn Treebank Nonterminals

S	Sentence or clause.	PP	Prepositional Phrase.
SBAR	Clause introduced by a (possibly empty) subordinating conjunction.	PRN	Parenthetical.
SBARQ	Direct question introduced by a <i>wh</i> -word or <i>wh</i> -phrase.	PRT	Particle.
SINV	Inverted declarative sentence.	QP	Quantity Phrase (i.e., complex measure/amount) within NP.
SQ	Inverted yes/no question, or main clause of a <i>wh</i> -question.	RRC	Reduced Relative Clause.
ADJP	Adjective Phrase.	UCP	Unlike Coordinated Phrase.
ADVP	Adverb Phrase.	VP	Verb Phrase.
CONJP	Conjunction Phrase.	WHADJP	<i>Wh</i> -adjective Phrase, as in <i>how hot</i> .
FRAG	Fragment.	WHADVP	<i>Wh</i> -adverb Phrase.
INTJ	Interjection.	WHNP	<i>Wh</i> -noun Phrase, e.g. <i>who</i> , <i>which book</i> , <i>whose daughter</i> , <i>none of which</i> , or <i>how many leopards</i> .
LST	List marker. Includes surrounding punctuation.	WHPP	<i>Wh</i> -prepositional Phrase, e.g., <i>of which</i> or <i>by whose authority</i> .
NAC	Not A Constituent; used within an NP.	X	Unknown, uncertain, or unbracketable.
NP	Noun Phrase.		
NX	Used within certain complex NPs to mark the head.		

# Syntactic Ambiguities

*Time flies like an arrow.*

*Fruit flies like a banana.*

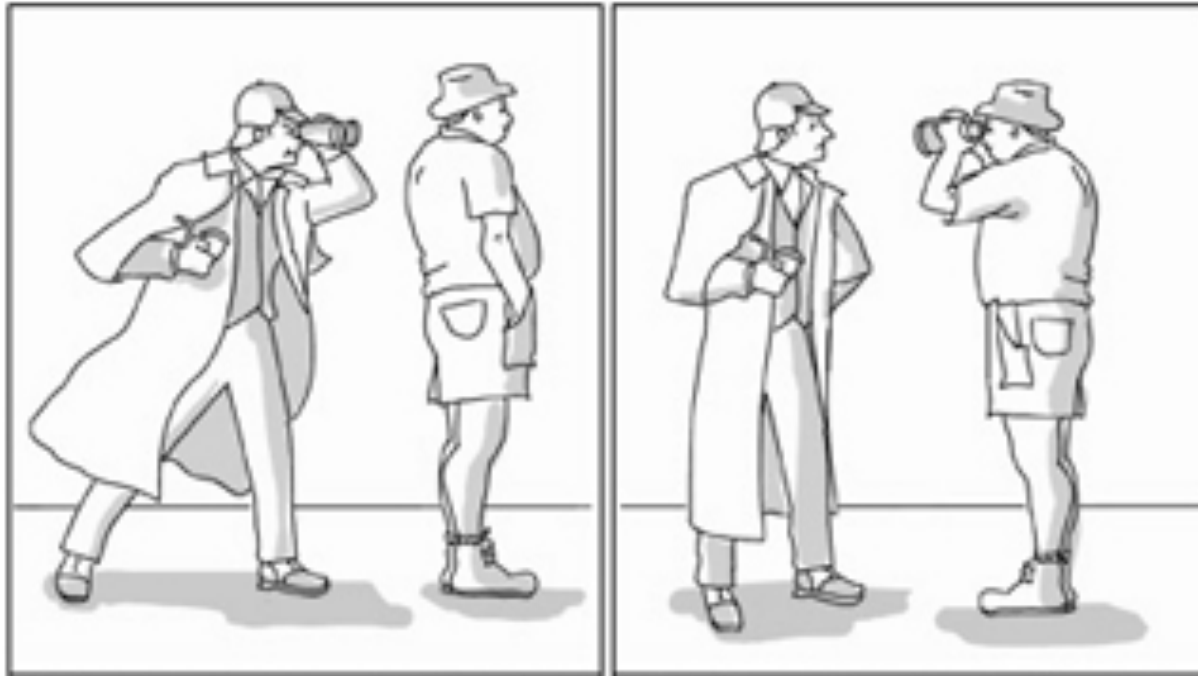




# Syntactic Ambiguities

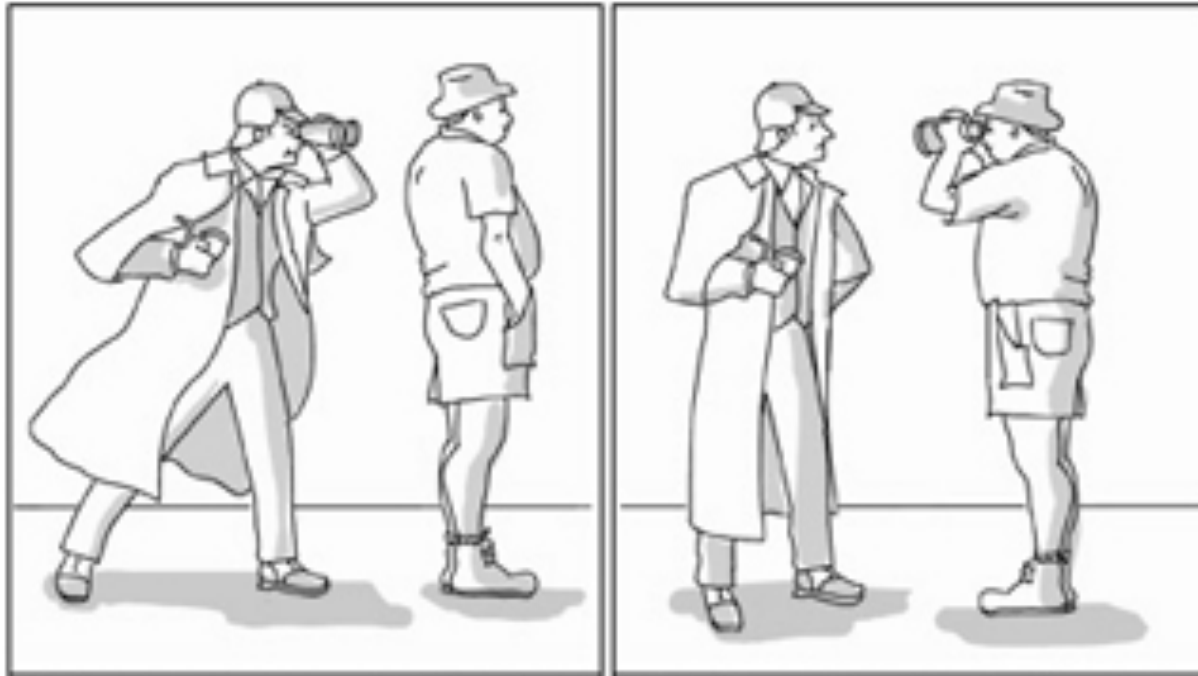
- attachment ambiguity
- coordination ambiguity
- noun compound ambiguity

# Attachment Ambiguity



Sherlock saw the man using binoculars

# Attachment Ambiguity



Sherlock (saw (the man) (using binoculars))

Sherlock (saw (the man (using binoculars)))

# other attachment ambiguities

Infant pulled from car involved in short police pursuit

Somali tied to militants held on U.S. ship for months

# other attachment ambiguities

(Infant pulled from car) involved in short police pursuit

Infant pulled from (car involved in short police pursuit)

(Somali tied to militants) held on U.S. ship for months

Somali tied to (militants held on U.S. ship for months)

# coordination ambiguities

- often found when modifiers are used with conjunctions:  
keyboard and monitor with the Apple logo

old men and women

# coordination ambiguities

- often found when modifiers are used with conjunctions:

(**keyboard and monitor**) with the Apple logo  
keyboard and (**monitor with the Apple logo**)

old (**men and women**)

(**old men**) and women

# noun compound ambiguity

- California history teacher
- World Trade Center
- student film society

Szymanek;  
Fromkin (2000);  
Spencer (1991)



# adjective/noun modifier ambiguity

- ancient history teacher
- moral philosophy professor
- indoor garden party

# NLP Task: Constituent Parsing

- given a sentence, output its constituent parse
- widely-studied task with a rich history
- most based on the Penn Treebank (Marcus et al.), developed at Penn in early 1990s



- Treebank = “corpus of annotated parse trees”

# How are constituent parses used?

- language modeling
  - predict the next word better by using syntactic structure
- machine translation
  - there are many syntactic translation models that require parsers for one or both languages
- text classification
  - for certain kinds of classification, features on syntactic fragments can help
- question answering, coreference resolution, etc.