# TTIC 31190: <br> Natural Language Processing 

Kevin Gimpel
Winter 2016

Lecture 3: Words

- Assignment 1 has been posted
- Due 11:59 pm on Wednesday, January 20 ${ }^{\text {th }}$
- We will start class 5 minutes late from now on, due to several students taking algorithms across campus
- My office hours are Mondays 3-4pm, \#531 (or by appointment)
- TA office hours are Thursdays 4-5pm, \#501
- If you're auditing, you may still turn in the homework and we will give you feedback (though we may not give your homework as much attention as others)
- If you didn't receive an email from me this details, then please email me with your name/email and let me know whether you are taking course for credit


## Today

- review of loss functions and subgradients from last week (useful for homework)
- start words (more about words and lexical semantics on Thursday)


## Empirical Risk Minimization with Surrogate Loss Functions

- given training data: $\mathcal{T}=\left\{\left\langle\boldsymbol{x}^{(i)}, y^{(i)}\right\rangle\right\}_{i=1}^{|\mathcal{T}|}$ where each $y^{(i)} \in \mathcal{L}$ is a label
- we want to solve the following:

$$
\hat{\boldsymbol{\theta}}=\underset{\boldsymbol{\theta}}{\operatorname{argmin}} \sum_{i=1}^{|\mathcal{T}|} \operatorname{loss}\left(\boldsymbol{x}^{(i)}, y^{(i)}, \boldsymbol{\theta}\right)
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& \hat{\boldsymbol{\theta}}=\underset{\boldsymbol{\theta}}{\operatorname{argmin}} \sum_{i=1}^{|\mathcal{T}|} \operatorname{loss}\left(\boldsymbol{x}^{(i)}, y^{(i)}, \boldsymbol{\theta}\right) \\
& \text { many possible loss } \\
& \text { functions to consider } \\
& \text { optimizing }
\end{aligned}
$$

## Cost Functions

- cost function: scores output against a gold standard

$$
\operatorname{cost}: \mathcal{L} \times \mathcal{L} \rightarrow \mathbb{R}_{\geq 0}
$$

- should reflect the evaluation metric for your task
- usual convention: $\operatorname{cost}(y, y)=0$


## Surrogate Loss Functions

cost loss / 0-1 loss: $\quad \operatorname{loss}_{\operatorname{cost}}(\boldsymbol{x}, y, \boldsymbol{\theta})=\operatorname{cost}(y, \operatorname{classify}(\boldsymbol{x}, \boldsymbol{\theta}))$
max-score loss:

$$
\operatorname{loss}_{\text {maxscore }}(\boldsymbol{x}, y, \boldsymbol{\theta})=-\operatorname{score}(\boldsymbol{x}, y, \boldsymbol{\theta})
$$

## Visualization


five possible outputs

## Visualization


five possible outputs

## Visualization



## Visualization



## Visualization


$\operatorname{loss}_{\text {maxscore }}(\boldsymbol{x}, y, \boldsymbol{\theta})=-\operatorname{score}(\boldsymbol{x}, y, \boldsymbol{\theta})$

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score

perceptron loss:
$\operatorname{loss}_{\text {perc }}(\boldsymbol{x}, y, \boldsymbol{\theta})=-\operatorname{score}(\boldsymbol{x}, y, \boldsymbol{\theta})+\max _{y^{\prime} \in \mathcal{L}} \operatorname{score}\left(\boldsymbol{x}, y^{\prime}, \boldsymbol{\theta}\right)$
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## effect of learning: gold standard will have highest score

hinge loss:
$\operatorname{loss}_{\text {hinge }}(\boldsymbol{x}, y, \boldsymbol{\theta})=-\operatorname{score}(\boldsymbol{x}, y, \boldsymbol{\theta})+\max _{y^{\prime} \in \mathcal{L}}\left(\operatorname{score}\left(\boldsymbol{x}, y^{\prime}, \boldsymbol{\theta}\right)+\operatorname{cost}\left(y, y^{\prime}\right)\right)$
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$$

## score + cost


$y_{1}$

$y_{2}$

effect of learning: score of gold standard
will be higher than score+cost of all others

## Subgradients of Loss Functions

- some of our loss functions are not differentiable:

$$
\operatorname{loss}_{\text {perc }}(\boldsymbol{x}, y, \boldsymbol{\theta})=-\sum_{i} \theta_{i} f_{i}(\boldsymbol{x}, y)+\max _{y^{\prime} \in \mathcal{L}} \sum_{i} \theta_{i} f_{i}\left(\boldsymbol{x}, y^{\prime}\right)
$$

- but they are subdifferentiable:


## Subgradient Examples

$$
f(x)=|x|=\max (x,-x)
$$



$$
\begin{array}{ll}
x<0: & \partial f(x)= \\
x>0: & \partial f(x)= \\
x=0: & \partial f(x)=
\end{array}
$$

## Subgradient Examples

$$
f(x)=|x|=\max (x,-x)
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$$
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& x<0: \quad \partial f(x)=\{-1\} \\
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## Subgradient Examples

$$
f(x)=|x|=\max (x,-x)
$$



- to find a subgradient of max of convexfunctions at a point, choose one function that achieves the max at that point and choose any of its subgradients at the point


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find subgradient of the
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\frac{\partial}{\partial \theta_{j}} \max _{y^{\prime} \in \mathcal{L}} \sum_{i} \theta_{i} f_{i}\left(\boldsymbol{x}, y^{\prime}\right)=\frac{\partial}{\partial \theta_{j}} \sum_{i} \theta_{i} f_{i}(\boldsymbol{x}, \operatorname{classify}(\boldsymbol{x}, \boldsymbol{\theta}))=f_{j}(\boldsymbol{x}, \operatorname{classify}(\boldsymbol{x}, \boldsymbol{\theta}))
$$

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## Roadmap

- classification
- words
- lexical semantics
- language modeling
- sequence labeling
- syntax and syntactic parsing
- neural network methods in NLP
- semantic compositionality
- semantic parsing
- unsupervised learning
- machine translation and other applications


## Words

- what is a word?
- tokenization
- morphology
- word sense


## What is a word?

## Tokenization

- tokenization: convert a character stream into words by adding spaces
- for certain languages, highly nontrivial
- e.g., Chinese word segmentation is a widelystudied NLP task


## Tokenization

- for other languages (English), tokenization is easier but is still not always obvious
- the data for your homework has been tokenized:
- punctuation has been split off from words
- contractions have been split


## Intricacies of Tokenization

- separating punctuation characters from words?
- , " ! $\rightarrow$ always separate
$-\quad . \quad$ when shouldn't we separate it?


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- Dr., Mr., Prof., U.S., etc.


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- ," ?! $\rightarrow$ always separate
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- Dr., Mr., Prof., U.S., etc.
- English contractions:
- isn't, aren't, wasn't,... $\rightarrow$ is n't, are n't, was n't,...
- but how about these: can't, won't $\rightarrow$ ca n't, wo n't
- ca and wo are then different forms from can and will
－Chinese and Japanese：no spaces between words：
- 莎拉波娃现在居住在美国东南部的佛罗里达。
- 莎拉波娃 现在 居住 在 美国 东南部 的 佛罗里达
－Sharapova now lives in US southeastern Florida
－Further complicated in Japanese，with multiple alphabets intermingled
－Dates／amounts in multiple formats


End－user can express query entirely in hiragana！

## Word Segmentation in Chinese

- Chinese words are composed of characters
- characters are generally 1 syllable and 1 morpheme
- average word is 2.4 characters long
- standard baseline segmentation algorithm:
- Maximum Matching (also called Greedy)


## Maximum Matching

Word Segmentation Algorithm

Given a Chinese word list and a string:

1) start a pointer at the beginning of the string
2) find longest word in dictionary that matches the string starting at pointer
3) move the pointer over the word in string
4) go to 2

## Maximum Matching Examples

－Thecatinthehat
－Thetabledownthere
the cat in the hat
the table down there theta bled own there
－Doesn＇t generally work in English！
－But works astonishingly well in Chinese

- 莎拉波娃现在居住在美国东南部的佛罗里达。
- 莎拉波娃 现在 居住 在 美国 东南部 的 佛罗里达
－Modern probabilistic segmentation algorithms even better


## Effect on Machine Translation

## Reference translation:

scientists complete sequencing of the chromosome linked to early dementia
CharBased segmented input:

MaxMatch segmented input:

Translation with CharBased segmentation:
scientists at the beginning of the stake of chile lost the genome sequence completed

## Translation with MaxMatch segmentation:

scientists at stake for the early loss of intellectual syndrome chromosome completed sequencing

## Removing Spaces?

- tokenization is usually about adding spaces
- but might we also want to remove spaces?
- what are some English examples?


## Removing Spaces?

- tokenization is usually about adding spaces
- but might we also want to remove spaces?
- what are some English examples?
- names?
- New York $\rightarrow$ NewYork
- non-compositional compounds?
- hot dog $\rightarrow$ hotdog
- other artifacts of our spacing conventions?
- New York-Long Island Railway


## Types and Tokens

- once text has been tokenized, let's count the words
- types: entries in the vocabulary
- tokens: instances of types in a corpus
- example sentence: If they want to go, they should go .
- how many types?
- how many tokens?


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- high type/token ratio $\rightarrow$ rich morphology
- low type/token ratio $\rightarrow$ poor morphology


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- in 1 million tweets, 15M tokens, 600k types
- in 56 million tweets, 847M tokens, ? types


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## How are words distributed?

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## Zipf’s Law

- also predicts other kinds of data: population of cities in a country, revenue of different companies, etc.


The Laurentian
University Sports Analytics Group

## The Long Tail

- there are so many word types!
- but words have internal structure


## Morphology

- morphemes:
- the small meaningful units that make up words
- stems: core meaning-bearing units
- affixes: bits and pieces that adhere to stems
- often with grammatical functions


## Kinds of Word Formation

- inflection: modifying a word with an affix to change its grammatical function (tense, number, etc.)
- result is a "different form of the same word"
- examples: book $\rightarrow$ books, walk $\rightarrow$ walked


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- derivation: adding an affix to a stem to create a new word
- examples: great $\rightarrow$ greatly, great $\rightarrow$ greatness
- compounding: combining two stems
- examples: lawsuit, keyboard, bookcase


## Morphology

- usually, morphological derivation is simply splitting a word into its morphemes:
- walked = walk + ed
- greatness $=$ great + ness
- but it can actually be a hierarchical structure


## Morphology

- ambiguity in hierarchical morphological decomposition?
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- what does this word mean?


## Morphology

- ambiguity in hierarchical morphological decomposition?
- rare, but it does happen
- unlockable $=$ un + lock + able
- what does this word mean?
- (un+lock)+able: "able to be unlocked"
- un+(lock+able): "unable to be locked"


## Morphology in NLP

- two common tasks:
- lemmatization
- stemming


## Lemmatization

- lemmatization: reduce inflections or variant forms to base form
- am, are, is $\rightarrow$ be
- car, cars, car's, cars' $\rightarrow$ car
- the boy's cars are different colors $\rightarrow$ the boy car be different color
- have to find correct dictionary headword form
- e.g., for machine translation:
- Spanish quiero ('I want'), quieres ('you want') same lemma as querer 'want'


## Stemming

- stemming: reduces words to their stems via crude chopping of affixes
- e.g., automate(s), automatic, automation all reduced to automat
- language dependent
- key step in information retrieval

> for example compressed and compression are both accepted as equivalent to compress.
for exampl compress and compress ar both accept as equival to compress

## Porter's algorithm

## The most common English stemmer

Step 1a

| sses | $\rightarrow$ ss | caresses | $\rightarrow$ caress |
| :--- | :--- | :--- | :--- |
| ies | $\rightarrow$ i | ponies | $\rightarrow$ poni |
| ss | $\rightarrow$ ss caress | $\rightarrow$ caress |  |
| $s$ | $\rightarrow \varnothing$ | cats | $\rightarrow$ cat |

Step 1b


Step 2 (for long stems)

```
ational-> ate relational }->\mathrm{ relate
izer-> ize digitizer }->\mathrm{ digitize
ator }->\mathrm{ ate operator }->\mathrm{ operate
```

Step 3 (for longer stems)


Viewing morphology in a corpus Why only strip -ing if there is a vowel?
$\begin{array}{rlr}(* v *) \text { ing } \rightarrow \varnothing \text { walking } & \rightarrow \text { walk } \\ \text { sing } & \rightarrow \text { sing }\end{array}$

# Viewing morphology in a corpus Why only strip -ing if there is a vowel? 

$$
\begin{array}{rlr}
(* v *) \text { ing } \rightarrow \varnothing \text { walking } & \rightarrow \text { walk } \\
\text { sing } & \rightarrow \text { sing }
\end{array}
$$

```
tr -sc 'A-Za-z' '\n' < shakes.txt | grep 'ing$' | sort | uniq -c | sort -nr
    1 3 1 2 ~ K i n g ~ 5 4 8 ~ b e i n g
    5 4 8 \text { being } 5 4 1 \text { nothing}
    5 4 1 \text { nothing } 1 5 2 \text { something}
    3 8 8 \text { king 145 coming}
    3 7 5 \text { bring } 1 3 0 \text { morning}
    3 5 8 \text { thing } 1 2 2 \text { having}
    3 0 7 \text { ring } 1 2 0 \text { living}
    152 something 117 loving
    145 coming 116 Being
    130 morning 102 going
tr -sc 'A-Za-z' '\n' < shakes.txt | grep '[aeiou].*ing$' | sort | uniq -c | sort -nr
```


## Dealing with complex morphology is sometimes necessary

- Some languages requires complex morpheme segmentation
- Turkish
- Uygarlastiramadiklarimizdanmissinizcasina: "(behaving) as if you are among those whom we could not civilize"
- Uygar `civilized’ + las `become'
+ tir `cause' + ama `not able'
+ dik `past' + lar 'plural'
+ imiz'p1pl' + dan 'abl'
+ mis 'past' + siniz '2pl' + casina 'as if'


## Terminology: lemma and wordform

- lemma or citation form
- same stem, part of speech, rough semantics
- wordform
- inflected word as it appears in text

| wordform | lemma |
| :---: | :---: |
| banks | bank |
| sung | sing |
| duermes | dormir |

